M.Sc Chemistry

Inorganic Special Paper
Semester IV

Course – 4101 B

Course Title – Spectral Techniques in Inorganic Chemistry

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Electron Paramagnetic Resonance Spectroscopy (EPR)

➢ Also Known as Electron Spin Resonance (ESR)

➢ EPR is a method for observing the behavior (dynamics) of the electrons within a suitable molecule, and for analyzing various phenomena by identifying the electron environment.

➢ EPR is a technique used to study chemical species with unpaired electrons

➢ EPR measurements afford information about the existence of unpaired electrons, as well as quantities, type, nature, environment and behavior.

➢ EPR instruments provide the only means of selectively measuring free radicals non-destructively and in any sample phase (gas, liquid or solid).

➢ EPR is actively being applied in pharmaceutical and agricultural basic research, and is widely used for various applications such as production lines for semiconductors and coatings, as well as in clinical and medical fields, such as cancer diagnosis.
Comparison between EPR and NMR

EPR is fundamentally similar to the more widely familiar method of NMR spectroscopy, with several important distinctions. While both spectroscopies deal with the interaction of electromagnetic radiation with magnetic moments of particles, there are many differences between the two spectroscopies:

1. EPR focuses on the interactions between an external magnetic field and the unpaired electrons of whatever system it is localized to, as opposed to the nuclei of individual atoms.

2. The electromagnetic radiation used in NMR typically is confined to the radio frequency range between 300 and 1000 MHz, whereas EPR is typically performed using microwaves in the 3 - 400 GHz range.

3. In EPR, the frequency is typically held constant, while the magnetic field strength is varied. This is the reverse of how NMR experiments are typically performed, where the magnetic field is held constant while the radio frequency is varied.
4. Due to the short relaxation times of electron spins in comparison to nuclei, EPR experiments must often be performed at very low temperatures, often below 10 K, and sometimes as low as 2 K. This typically requires the use of liquid helium as a coolant.

5. EPR spectroscopy is inherently roughly 1,000 times more sensitive than NMR spectroscopy due to the higher frequency of electromagnetic radiation used in EPR in comparison to NMR.

It should be noted that advanced pulsed EPR methods are used to directly investigate specific couplings between paramagnetic spin systems and specific magnetic nuclei. The most widely application is Electron Nuclear Double Resonance (ENDOR). In this method of EPR spectroscopy, both microwave and radio frequencies are used to perturb the spins of electrons and nuclei simultaneously in order to determine very specific couplings that are not attainable through traditional continuous wave methods.
Electron Paramagnetic Resonance (EPR), also called Electron Spin Resonance (ESR), is a branch of magnetic resonance spectroscopy which utilizes microwave radiation to probe species with unpaired electrons, such as radicals, radical cations, and triplets in the presence of an externally applied static magnetic field. In many ways, the physical properties for the basic EPR theory and methods are analogous to Nuclear Magnetic Resonance (NMR). The most obvious difference is that the direct probing of electron spin properties in EPR is opposed to nuclear spins in NMR. Although limited to substances with unpaired electron spins, EPR spectroscopy has a variety of applications, from studying the kinetics and mechanisms of highly reactive radical intermediates to obtaining information about the interactions between paramagnetic metal clusters in biological enzymes. EPR can even be used to study the materials with conducting electrons in the semiconductor industry.

EPR is a remarkably useful form of spectroscopy used to study molecules or atoms with an unpaired electron. It is less widely used than NMR because stable molecules often do not have unpaired electrons. However, EPR can be used analytically to observe labeled species in situ either biologically or in a chemical reaction.
Historical Development of EPR

In 1896, the line splitting in optical spectra in a static magnetic field was first found by a Dutch physicist Zeeman. In 1920s, Stern and Gerlach sent a beam of silver atoms through an inhomogeneous magnetic field and the beam splits into two distinct parts, indicating the intrinsic angular momentum of electrons and atoms. Then Uhlenbeck and Goudsmit proposed that the electrons have an angular momentum. In 1938, Isidor Rabi measured the magnetic resonance absorption of lithium chloride molecules, which means he could measure different resonances to get more detailed information about molecular structure. After World War II, microwave instrumentation’s widespread availability sped up the development of electron paramagnetic resonance (EPR). The first observation of a magnetic resonance signal was detected by a Soviet physicist Zavoisky in several salts, including hydrous copper chloride, copper sulfate and manganese sulfate in 1944. Later the Oxford group proposed the basic theory of magnetic resonance. Contributed by many researchers, such as Cummerow & Halliday and Bagguley & Griffiths, EPR was extensively studied. Between 1960 and 1980, continuous wave (CW) EPR was developed and pulsed EPR was mainly studied in Bell laboratories. EPR was usually applied for organic free radicals. In the 1980s, the first commercial pulsed EPR spectrometer appeared in the market and was then extensively used for biological, medical field, active oxygen and so on. Nowadays, EPR has become a versatile and standard research tool.
The sample is held in a very strong magnetic field, while electromagnetic (EM) radiation is applied monochromatically.

Figure: Monochromatic electromagnetic beam
This portion of EPR is analogous to simple spectroscopy, where absorbance by the sample of a single or range of wavelengths of EM radiation is monitored by the end user i.e. absorbance. The unpaired electrons can either occupy $+\frac{1}{2}$ or $-\frac{1}{2}$ $m_s$ value (Figure). From here either the magnetic field $B_o$ is varied or the incident light is varied. Today most researchers adjust the EM radiation in the microwave region, the theory is the find the exact point where the electrons can jump from the less energetic $m_s = -\frac{1}{2}$ to $m_s = +\frac{1}{2}$. More electrons occupy the lower $m_s$ value.

Figure: Resonance of a free electron.
Overall, there is an absorption of energy. This absorbance value, when paired with the associated wavelength can be used in the equation to generate a graph of showing how absorption relates to frequency or magnetic field.

$$\Delta E = h\nu = g_e\beta_B B_0$$

where $g_e$ equals to 2.0023193 for a free electron; $\beta_B$ is the Bohr magneton and is equal to 9.2740 * 10^{-24} JT^{-1}; and $B_0$ indicates the external magnetic field.
Like most spectroscopic techniques, EPR spectrometers measure the absorption of electromagnetic radiation. A simple absorption spectra will appear similar to the one on the top of Figure. However, a phase-sensitive detector is used in EPR spectrometers which converts the normal absorption signal to its first derivative. Then the absorption signal is presented as its first derivative in the spectrum, which is similar to the one on the bottom of Figure. Thus, the magnetic field is on the x-axis of EPR spectrum; $d\chi''/dB$, the derivative of the imaginary part of the molecular magnetic susceptibility with respect to the external static magnetic field in arbitrary units is on the y-axis. In the EPR spectrum, where the spectrum passes through zero corresponds to the absorption peak of absorption spectrum. People can use this to determine the center of the signal. On the x-axis, sometimes people use the unit “gauss” (G), instead of tesla (T). One tesla is equal to 10000 gauss.
Figure: Comparison of absorption spectrum and EPR spectrum.
Like NMR, EPR can be used to observe the geometry of a molecule through its magnetic moment and the difference in electron and nucleus mass. EPR has mainly been used for the detection and study of free radical species, either in testing or analytical experimentation. "Spin labeling" species of chemicals can be a powerful technique for both quantification and investigation of otherwise invisible factors.

The EPR spectrum of a free electron, there will be only one line (one peak) observed. But for the EPR spectrum of hydrogen, there will be two lines (2 peaks) observed due to the fact that there is interaction between the nucleus and the unpaired electron. This is also called *hypersine splitting*. The distance between two lines (two peaks) are called *hypersine splitting constant (A)*.

By using \((2Nl+1)\), we can calculate the components or number of hypersine lines of a multiplet of a EPR transition, where \(N\) indicates number of spin, \(l\) indicates number of equivalent nuclei. For example, for nitrooxide radicals, the nuclear spin of \(^{14}\text{N}\) is 1, \(N=1\), \(l=1\), we have \(2 \times 1 + 1 = 3\), which means that for a spin 1 nucleus splits the EPR transition into a triplet.
To absorb microwave, there must be unpaired electrons in the system. No EPR signal will be observed if the system contains only paired electrons since there will be no resonant absorption of microwave energy. Molecules such as NO, NO$_2$, O$_2$ do have unpaired electrons in ground states. EPR can be also performed on proteins with paramagnetic ions such as Mn$^{2+}$, Fe$^{3+}$ and Cu$^{2+}$. Additionally, molecules containing stable nitrooxide radicals such as 2,2,6,6-tetramethyl-1-piperidinyloxyl (TEMPO) and di-tert-butyl nitrooxide radical.

Figure: The nitrooxide radical TEMPO
Proportionality Factor (g Factor)

As a result of the Zeeman Effect, the state energy difference of an electron with $s=\frac{1}{2}$ in magnetic field is

$$\Delta E = g\beta B \quad \text{... (1)}$$

where $\beta$ is the constant, Bohr magneton. Since the energy absorbed by the electron should be exactly the same with the state energy difference $\Delta E$, $\Delta E=\hbar\nu$ ($\hbar$ is Planck’s constant), the Equation can be expressed as

$$\hbar\nu = g\beta B \quad \text{... (2)}$$

People can control the microwave frequency $\nu$ and the magnetic field $B$. The other factor, $g$, is a constant of proportionality, whose value is the property of the electron in a certain environment. After plugging in the values of $\hbar$ and $\beta$ in Equation 2, $g$ value can be given through Equation 3:

$$g = 71.4484\nu (\text{in GHz})/B (\text{in mT}) \quad \text{... (3)}$$
A free electron in vacuum has a $g$ value $g = 2.00232$. For instance, at the magnetic field of 331.85 mT, a free electron absorbs the microwave with an X-band frequency of 9.300 GHz. However, when the electron is in a certain environment, for example, a transition metal-ion complex, the second magnetic field produced by the nuclei, $\Delta B$, will also influence the electron. At this kind of circumstance, Equation 2 becomes

$$h\nu = g\beta(B_e + \Delta B)$$

... (4)

since we only know the spectrometer value of $B$, the Equation 4 is written as:

$$h\nu = (g_e + \Delta g)\beta B$$

... (5)

From the relationship shown above, we know that there are infinite pairs of $\nu$ and $B$ that fit this relationship. The magnetic field for resonance is not a unique "fingerprint" for the identification of a compound because spectra can be acquired at different microwave frequencies. Then what is the fingerprint of a molecule? It is $\Delta g$. This value contains the chemical information that lies in the interaction between the electron and the electronic structure of the molecule, one can simply take the value of $g = g_e + \Delta g$ as a fingerprint of the molecule.
For organic radicals, the g value is very close to $g_e$ with values ranging from 1.99-2.01. For example, the g value for •CH$_3$ is 2.0026. For transition metal complexes, the g value varies a lot because of the spin-orbit coupling and zero-field splitting. Usually it ranges from 1.4-3.0, depending on the geometry of the complex. For instance, the g value of Cu(acac)$_2$ is 2.13. To determine the g value, we use the center of the signal. By using Equation 3, we can calculate the g factor of the absorption in the spectrum. The value of g factor is not only related to the electronic environment, but also related to anisotropy.

Figure: EPR spectra of some proteins
An electron is a negatively charged particle with certain mass, it mainly has two kinds of movements. The first one is spinning around the nucleus, which brings orbital magnetic moment. The other is "spinning" around its own axis, which brings spin magnetic moment. Magnetic moment of the molecule is primarily contributed by unpaired electron's spin magnetic moment.

\[
M_s = \sqrt{S(S + 1)}h/2\pi
\]

\(M_s\) is the total spin angular moment,
\(S\) is the spin quantum number and
\(h\) is Planck's constant.

In the z direction, the component of the total spin angular moment can only assume two values:

\[
M_{sz} = m_s.h/2\pi
\]

The term \(m_s\) have \((2S + 1)\) different values: \(+S, (S - 1), (S - 2), \ldots, -S\). For single unpaired electron, only two possible values for \(m_s\) are \(+1/2\) and \(-1/2\).
The magnetic moment, $\mu_e$ is directly proportional to the spin angular momentum and one may therefore write

$$\mu_e = -g_e \mu_B M_S$$

The appearance of negative sign due to the fact that the magnetic momentum of electron is collinear, but antiparallel to the spin itself. The term $(g_e \mu_B)$ is the magnetogyrlic ratio. The Bohr magneton, $\mu_B$, is the magnetic moment for one unit of quantum mechanical angular momentum:

$$\mu_B = \frac{e\hbar}{4\pi m_e}$$

where $e$ is the electron charge, $m_e$ is the electron mass, the factor $g_e$ is known as the free electron g-factor with a value of 2.002 319 304 386 (one of the most accurately known physical constant). This magnetic moment interacts with the applied magnetic field. The interaction between the magnetic moment ($\mu$) and the field ($B$) is described by

$$E = -\mu \cdot B$$

For single unpaired electron, there will be two possible energy states, this effect is called Zeeman splitting.
Origin of the EPR Signal (Contd…)

\[ E_{+1/2} = \frac{1}{2} (g\mu_B B) \]

\[ E_{-1/2} = -\frac{1}{2} (g\mu_B B) \]

In the absence of external magnetic field,

\[ E_{+1/2} = E_{-1/2} = 0 \]

However, in the presence of external magnetic field, the difference between the two energy states can be written as

\[ \Delta E = h\nu = g\mu_B B \]

Fig.: Energy levels for an electron spin \( M_S = \pm 1/2 \) in an applied magnetic field \( B \)
With the intensity of the applied magnetic field increasing, the energy difference between the energy levels widens until it matches with the microwave radiation, and results in absorption of photons. This is the fundamental basis for EPR spectroscopy. EPR spectrometers typically vary the magnetic field and hold the microwave frequency. EPR spectrometers are available in several frequency ranges, and X band is currently the most commonly used.

<table>
<thead>
<tr>
<th>Microwave Band</th>
<th>Frequency/GHz</th>
<th>Wavelength/cm</th>
<th>B(electron)/Tesla</th>
</tr>
</thead>
<tbody>
<tr>
<td>S</td>
<td>3.0</td>
<td>10.0</td>
<td>0.107</td>
</tr>
<tr>
<td>X</td>
<td>9.5</td>
<td>3.15</td>
<td>0.339</td>
</tr>
<tr>
<td>K</td>
<td>23</td>
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<tr>
<td>Q</td>
<td>35</td>
<td>0.86</td>
<td>1.25</td>
</tr>
<tr>
<td>W</td>
<td>95</td>
<td>0.315</td>
<td>3.3</td>
</tr>
</tbody>
</table>

Table: Different Microwave bands for EPR Spectroscopy
EPR is often used to investigate systems in which electrons have both orbital and spin angular momentum, which necessitates the use of a scaling factor to account for the coupling between the two momenta. This factor is the g-factor, and it is roughly equivalent in utility how chemical shift is used in NMR. The g factor is associated with the quantum number $J$, the total angular momentum, where $J = L + S$.

$$g_J = \frac{J(J+1)(g_L + g_s) + (L(L+1) - S(S+1))(g_L - g_s)}{2J(J+1)}$$

Here, $g_L$ is the orbital g value and $g_s$ is the spin g value. For most spin systems with angular and spin magnetic momenta, it can be approximated that $g_L$ is exactly 1 and $g_s$ is exactly 2. This equation reduces to what is called the Landé formula:

$$g_J = \frac{3}{2} - \frac{L(L+1) - S(S+1))}{2J(J+1)}$$

And the resultant electronic magnetic dipole is:

$$\mu_J = -g_J \mu_B J$$
In practice, these approximations do not always hold true, as there are many systems in which J-coupling does occur, especially in transition metal clusters where the unpaired spin is highly delocalized over several nuclei. But for the purposes of an elementary examination of EPR theory it is useful for the understanding of how the g factor is derived. In general this is simply referred to as the g-factor or the Landé g-factor.

The g-factor for a free electron with zero angular momentum still has a small quantum mechanical corrective value, with $g=2.0023193$. In addition to considering the total magnetic dipole moment of a paramagnetic species, the g-value takes into account the local environment of the spin system. The existence of local magnetic fields produced by other paramagnetic species, electric quadrupoles, magnetic nuclei, ligand fields (especially in the case of transition metals) all can change the effective magnetic field that the electron experiences such that

$$B_{eff} = B_0 + B_{local}$$
These local fields can either:

1. be induced by the applied field, and hence have magnitude dependence on $B_0$ or are
2. permanent and independent of $B_0$ other than in orientation.

In the case of the first type, it is easiest to consider the effective field experienced by the electron as a function of the applied field, thus we can write:

$$B_{eff} = B_0(1 - \sigma)$$

where $\sigma$ is the shielding factor that results in decreasing or increasing the effective field. The g-factor must then be replaced by a variable g factor $g_{eff}$ such that:

$$B_{eff} = B_0 \cdot \left( \frac{g}{g_{eff}} \right)$$
Many organic radicals and radical ions have unpaired electrons with \( L \) near zero, and the total angular momentum quantum number \( J \) becomes approximately \( S \). As a result, the \( g \)-values of these species are typically close to 2. In stark contrast, unpaired spins in transition metal ions or complexes typically have larger values of \( L \) and \( S \), and their \( g \) values diverge from 2 accordingly.

\[
E_{m_s} = m_s g_e \mu_B B_0
\]

After all of this, the energy levels that correspond to the spins in an applied magnetic field can now be written as:

\[
\Delta E_{m_s} = \Delta m_s g_e \mu_B B
\]

And thus the energy difference associated with a transition is given as:

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Typically, EPR is performed perpendicular mode, where the magnetic field component of the microwave radiation is oriented perpendicular to the magnetic field created by the magnet. Here, the selection rule for allowed EPR transitions is \( \Delta m_s = \pm 1 \), so the energy of the transition is simply:

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There is a method called Parallel Mode EPR in which the microwaves are applied parallel to the magnetic field, changing the selection rule to \( \Delta m_s = \pm 1 \).
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After all of this, the energy levels that correspond to the spins in an applied magnetic field can now be written as:

\[ E_{m_s} = m_s g_e \mu_B B_0 \]

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There is a method called Parallel Mode EPR in which the microwaves are applied parallel to the magnetic field, changing the selection rule to \( \Delta m_s = \pm 1 \).
Sensitivity

At the thermal equilibrium and external applied magnetic field, the spin population is split between the two Zeeman levels (Figure) according to the Maxwell–Boltzmann law. Absorption can occur as long as the number of particles in the lower state is greater than the number of particles in the upper state. At equilibrium, the ratio predicted by the Boltzmann distribution:

$$\frac{N_{\text{upper}}}{N_{\text{lower}}} = e^{-\frac{\Delta E}{k_B T}} = e^{\frac{g \mu B}{k_B T}}$$

with $k_B$ is the Boltzmann constant.

At regular temperatures and magnetic fields, the exponent is very small and the exponential can be accurately approximated by the expansion,

$$e^{-x} \approx 1 - x$$

Thus

$$\frac{N_{\text{upper}}}{N_{\text{lower}}} = 1 - \frac{g \mu B}{k_B T}$$
At 298 K in a field of about 3000 G the distribution shows that $N_{\text{upper}}/N_{\text{lower}} = 0.9986$, which means the difference between is $N_{\text{upper}}$ and $N_{\text{lower}}$ is very small. The populations of the two Zeeman levels are nearly the same, but the slight excess in the lower level gives rise to a net absorption.

\[
N_{\text{lower}} - N_{\text{upper}} = N_{\text{lower}} \left[ 1 - \left( 1 - \frac{g\mu B}{k_B T} \right) \right] = \frac{Ng\mu B}{2k_B T}
\]

This expression tells us that EPR sensitivity (net absorption) increases as temperature decreases and magnetic field strength increases, and magnetic field is proportional to microwave frequency. Theoretically speaking, the sensitivity of spectrometer with K-band or Q-band or W-band shoulder be greater than spectrometer with X-band. However, since the K-, Q- or W-band waveguides are smaller, samples are necessarily smaller, thus canceling the advantage of a more favorable Boltzmann factor.
Spin Operators and Hamiltonians

Any system which has discrete energy levels and is described by defined quantum numbers can be represented by an eigenvalue equation, such that if we define an operator ($\hat{\Lambda}$) that is appropriate to the property being observed, the eigenfunction equation is:

$$\hat{\Lambda}\psi_k = \lambda_k \psi_k$$

Here $\lambda_k$ is an eigenvalue of a state “k” for which the eigenfunction is $\psi_k$. EPR is most concerned with the quantization of spin angular momentum, therefore, the operator must be defined is a spin operator that operated on a function that describes a spin state. In the case of a system with a total electron spin of $S = \frac{1}{2}$, the two states are described by the quantum numbers $M_s = +1/2$ and $M_s = -1/2$, which measure the components $M_s$ of angular momentum along the z-direction of the magnetic field. In most systems, it is convenient to treat the direction of the magnetic field as the z-direction, and thus the spin operator is denoted $\hat{S}_z$, where $\hat{S}$ is the angular momentum operator. So, omitting the k index, the z-component of the angular momentum operator can be written as:

$$\hat{S}_z \phi_e = M_s \phi_e$$
where \( m \) is the eigenvalue of the operator \( S_z \), and \( \phi_e(M_s) \) is the corresponding eigenfunction. Adopting the \( \alpha \)-notation for spin states, where \( \alpha(e) = \phi_e(M_s=+1/2) \) and \( \beta(e) = \phi_e(M_s=-1/2) \), this expression can be written:

\[
\hat{S}_z \alpha (e) = +\frac{1}{2} \alpha (e) \\
\hat{S}_z \beta (e) = -\frac{1}{2} \beta (e)
\]

In a similar fashion, the eigenfunctions for the nuclear spin operator for a nucleus with spin = ½ can be written:

\[
\hat{I}_z \alpha (n) = +\frac{1}{2} \alpha (n) \\
\hat{I}_z \beta (n) = -\frac{1}{2} \beta (n)
\]

Written in the convenient Dirac notation, these expressions become:

\[
\hat{S}_z |\alpha (e)\rangle = +\frac{1}{2} |\alpha (e)\rangle \\
\hat{S}_z |\beta (e)\rangle = +\frac{1}{2} |\beta (e)\rangle
\]
Spin Operators and Hamiltonians (Contd…)

and

\[ \hat{I}_z |\alpha(n)\rangle = +\frac{1}{2} |\alpha(n)\rangle \]
\[ \hat{I}_z |\beta(n)\rangle = +\frac{1}{2} |\beta(n)\rangle \]

Using the time-independent Schrödinger equation, we can define the energies associated with the systems described by these equations as such:

\[ \hat{H}_e |\phi_{ek}\rangle = E_{ek} |\phi_{ek}\rangle \]
\[ \hat{H}_n |\phi_{nk}\rangle = E_{nk} |\phi_{nk}\rangle \]

So that

\[ \hat{H}_e |\alpha(e)\rangle = E_{\alpha(e)} |\alpha(e)\rangle \]
\[ \hat{H}_e |\beta(e)\rangle = E_{\alpha(e)} |\beta(e)\rangle \]
\[ \hat{H}_n |\alpha(n)\rangle = E_{\alpha(n)} |\alpha(n)\rangle \]
\[ \hat{H}_n |\beta(n)\rangle = E_{\alpha(n)} |\beta(n)\rangle \]

Here \(\hat{H}\) is the Hamiltonian operator and represents the operator for the total energy, and commutes with both I and S operators.
Using the Hamiltonians derived in the last section, we can develop Hamiltonians for the perturbed case in which an external magnetic field is introduced. For the simple case of the hydrogen atom with $S=1/2$ and $I=1/2$, interaction with a strong magnetic field oriented along the $z$-direction will be considered. Using the operator form, the Hamiltonian takes the form:

$$ \hat{H} = -B \hat{\mu}_z $$

Here, the electron magnetic moment operator $\mu_{ez}$ is proportional to the electron spin operator. Likewise, the nuclear magnetic moment operator $\mu_{nz}$ is proportional to the nuclear spin operator $I_z$. Therefore,

$$ \hat{\mu}_{ez} = \gamma_e \hat{S}_z \hbar = -g \mu_B \hat{S}_z $$
$$ \hat{\mu}_{nz} = \gamma_n \hat{I}_z \hbar = +g_n \mu_n \hat{I}_z $$

Now the electron and nuclear spin Hamiltonians can be defined as:

$$ \hat{H}_e = g_e \mu_B \hat{S}_z $$
$$ \hat{H}_n = -g_n \mu_n \hat{I}_z $$
According to the figure below, we should observe one spectra line in a paramagnetic molecule, but in reality, we usually observe more than one split line. The reason for that is hyperfine interactions, which results from interaction of the magnetic moment of the unpaired electron and the magnetic nuclei. The hyperfine patterns are highly valuable when it comes to determine the spatial structure of paramagnetic species and identify the paramagnetic species. As a result, nuclear spins act as probes which are sensitive to the magnitude and direction of the field due to the unpaired electron.

In general, there are two kinds of hyperfine interactions between unpaired electron and the nucleus. The first is the interaction of two dipoles. We refer it as the anisotropic or dipolar hyperfine interaction, which is the interaction between electron spin magnetic moment and the nuclei magnetic moment, and it depends on the shape of electronic orbital and the average distance of electron and nucleus. This interaction can help us to determine the possible position of a paramagnetic species in a solid lattice.
The second interaction is known as the Fermi contact interaction, and only takes the electrons in s orbital into consideration, since p, d and f orbitals have nodal planes passing through the nucleus. We refer to this type of interaction as isotropic, which depends on the presence of a finite unpaired electron spin density at the position of the nucleus, not on the orientation of the paramagnetic species in the magnetic field.

\[
A = -\frac{8}{3} \pi \langle \mu_n \cdot \mu_e \rangle \cdot |\psi(0)|^2
\]

A is the isotropic hyperfine coupling constant and is related to the unpaired spin density, \( \mu_n \) is the nuclear magnetic moment, \( \mu_e \) is the electron magnetic moment and \( \Psi(0) \) is the electron wavefunction at the nucleus. The Fermi contact interaction happens in s orbital when electron density is not zero. Thus nuclear hyperfine spectra not only includes the interaction of nuclei and their positions in the molecule but also the extent to which part or all of the molecule is free to reorientate itself according to the direction of the applied magnetic field.
In the case of one unpaired electron, the spin Hamiltonian can be written as below for the isotropic part of nuclear hyperfine interaction.

\[ H = H_{EZ} - H_{NZ} - H_{HFS} \]

EZ means electron Zeeman, NZ means nuclear Zeeman and HFS represents hyperfine interaction. The equation can also be written as

\[ \hat{H} = g\mu_B H S_Z - g_N \mu_N \cdot B I_Z + h \cdot S \cdot a I \]

The term \( aS*I \) is introduced by Fermi contact interaction. I is the nucleus spin, H is the external field. Since \( \mu_B \) is much larger than \( \mu_N \), the equation can take the form as:

\[ \hat{H} = g\mu_B H S_Z + h \cdot S \cdot a I \]
Isotropic Hyperfine Interactions

When one unpaired electron interacts with one nucleus, the number of EPR lines is $2I+1$. When one unpaired electron interacts with $N$ equivalent nuclei, the number of EPR lines is $2NI+1$. When one electron interacts with non-equivalent nuclei's ($N_1, N_2$, .....), the number of EPR lines is

$$\prod_{i=1}^{k} (2N_i I_i + 1)$$

In the case of DPPH, $I=1$ and two nitrogen nuclei are equivalent. $2NI+1=5$, we can get five lines: 1:2:3:2:1.

The structure of DPPH
The table below shows the relative intensities of the lines according to unpaired electrons interacting with multiple equivalent nuclei.

<table>
<thead>
<tr>
<th>Number of Equivalent Nuclei</th>
<th>Relative Intensities</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1:1</td>
</tr>
<tr>
<td>2</td>
<td>1:2:1</td>
</tr>
<tr>
<td>3</td>
<td>1:3:3:1</td>
</tr>
<tr>
<td>4</td>
<td>1:4:6:4:1</td>
</tr>
<tr>
<td>5</td>
<td>1:5:10:10:5:1</td>
</tr>
</tbody>
</table>

We can observe that increasing number of nucleuses leads to the complexity of the spectrum, and spectral density depends on the number of nuclei as equation shown below:

\[
Spectral\text{density}_{EPR} = \frac{\prod_{i=1}^{k} 2N_iI_i + 1}{\sum_{i=1}^{k} 2|\alpha_i|N_iI_i}
\]

\(\alpha\) is the isotropic hyperfine coupling constant.
The g Anisotropy

From the below equation, we can calculate g in this way:

\[ \Delta E = h\nu = g\mu_B B \]

If the energy gap is not zero, g factor can be remembered as:

\[ g \approx \frac{1}{14} \frac{\nu [GHZ]}{B [T]} \]

The g factor is not necessarily isotropic and needs to be treated as a tensor g. For a free electron, g factor is close to 2. If electrons are in the atom, g factor is no longer 2, spin orbit coupling will shift g factor from 2. If the atom are placed at an electrostatic field of other atoms, the orbital energy level will also shift, and the g factor becomes anisotropic. The anisotropies lead to line broadening in isotropic ESR spectra. The Electron-Zeeman interaction depends on the absolute orientation of the molecule with respect to the external magnetic field. Anisotropic is very important for free electrons in non-symmetric orbitals (p,d).
The $g$ Anisotropy (Contd…)

In a more complex spin system, Hamiltonian is required to interpret as below:

$$\hat{H}_s = \mu_B \vec{B} \cdot \vec{g} \cdot \hat{S} + \sum_i \vec{I}_i \cdot \vec{A}_i \cdot \hat{S}$$

g and $A_i$ are $3*3$ matrices representing the anisotropic Zeeman and nuclear hyperfine interactions, thus it is more accurate to describe $g$-factor as a tensor like:

$$g = \sqrt{g_x^2 \cdot \sin^2 \alpha \cdot \cos^2 \beta + g_y^2 \cdot \sin^2 \alpha \cdot \cos^2 \beta + g_z^2 \cdot \cos^2 \alpha}$$

Alpha and beta is the angle between magnetic field with respect to principle axis of g tensor. If $g_x = g_y$, it can be expressed as:

$$g = \sqrt{g_x^2 \cdot \sin^2 \alpha + g_z^2 \cdot \cos^2 \alpha}$$

Thus, we can identify the $g$ tensor by measuring the angular dependence in the above equation.
Another very important factor in EPR is hyperfine interactions. Besides the applied magnetic field $B_0$, the compound contains the unpaired electrons are sensitive to their local “micro” environment. Additional information can be obtained from the so called hyperfine interaction. The nuclei of the atoms in a molecule or complex usually have their own fine magnetic moments. Such magnetic moments occurrence can produce a local magnetic field intense enough to affect the electron. Such interaction between the electron and the nuclei produced local magnetic field is called the *hyperfine interaction*. Then the energy level of the electron can be expressed as:

$$E = g m_B B_0 M_S + a M_s m_I$$

In which $a$ is the hyperfine coupling constant, $m_I$ is the nuclear spin quantum number. Hyperfine interactions can be used to provide a wealth of information about the sample such as the number and identity of atoms in a molecule or compound, as well as their distance from the unpaired electron.
The rules for determining which nuclei will interact are the same as for NMR. For isotopes which have even atomic and even mass numbers, the ground state nuclear spin quantum number, \( I \), is zero, and these isotopes have no EPR (or NMR) spectra. For isotopes with odd atomic numbers and even mass numbers, the values of \( I \) are integers. For example the spin of \(^2\text{H}\) is 1. For isotopes with odd mass numbers, the values of \( I \) are fractions. For example the spin of \(^1\text{H}\) is \( 1/2 \) and the spin of \(^{23}\text{Na}\) is \( 7/2 \).

**Table. Bio transition metal nuclear spins and EPR hyperfine patterns**

<table>
<thead>
<tr>
<th>Metal</th>
<th>Valency</th>
<th>Isotope</th>
<th>Spin (abundance)</th>
<th>EPR lines</th>
</tr>
</thead>
<tbody>
<tr>
<td>V</td>
<td>IV</td>
<td>51</td>
<td>7/2</td>
<td>8</td>
</tr>
<tr>
<td>Mn</td>
<td>II</td>
<td>55</td>
<td>5/2</td>
<td>6</td>
</tr>
<tr>
<td>Fe</td>
<td>III</td>
<td>54, 56, 57, 58</td>
<td>0 + 1/2 (2%)</td>
<td>1 + 2 (1%)</td>
</tr>
<tr>
<td>Co</td>
<td>II</td>
<td>59</td>
<td>7/2</td>
<td>8</td>
</tr>
<tr>
<td>Ni</td>
<td>III, I</td>
<td>58, 60, 61, 62, 64</td>
<td>0 + 3/2 (1%)</td>
<td>1 + 4 (0.25%)</td>
</tr>
<tr>
<td>Cu</td>
<td>II</td>
<td>63, 65</td>
<td>3/2</td>
<td>4</td>
</tr>
<tr>
<td>Mo</td>
<td>V</td>
<td>92, 94, 95, 96, 97, 98, 100</td>
<td>0 + 5/2 (25%)</td>
<td>1 + 6 (4%)</td>
</tr>
<tr>
<td>W</td>
<td>V</td>
<td>180, 182, 183, 184, 186</td>
<td>0 + 1/2 (14%)</td>
<td>1 + 2 (7%)</td>
</tr>
</tbody>
</table>
**Table. Bio ligand atom nuclear spins and their EPR hyperfine patterns**

<table>
<thead>
<tr>
<th>Ligand</th>
<th>Isotope</th>
<th>Spin (abundance)</th>
<th>EPR lines</th>
</tr>
</thead>
<tbody>
<tr>
<td>H</td>
<td>1, 2</td>
<td>1/2 + 1 (0.015%)</td>
<td>2 + 3</td>
</tr>
<tr>
<td>C</td>
<td>12, 13</td>
<td>0 + 1/2 (1.1%)</td>
<td>1 + 2</td>
</tr>
<tr>
<td>N</td>
<td>14, 15</td>
<td>1 + 1/2 (0.4%)</td>
<td>3 + 2</td>
</tr>
<tr>
<td>O</td>
<td>16, 17, 18</td>
<td>0 + 5/2 (0.04%)</td>
<td>1 + 6</td>
</tr>
<tr>
<td>F</td>
<td>19</td>
<td>1/2</td>
<td>2</td>
</tr>
<tr>
<td>P</td>
<td>31</td>
<td>1/2</td>
<td>2</td>
</tr>
<tr>
<td>S</td>
<td>32, 33, 34</td>
<td>0 + 3/2 (0.8%)</td>
<td>1 + 4</td>
</tr>
<tr>
<td>Cl</td>
<td>35, 37</td>
<td>3/2</td>
<td>4</td>
</tr>
<tr>
<td>As</td>
<td>75</td>
<td>3/2</td>
<td>4</td>
</tr>
<tr>
<td>Se</td>
<td>76, 77, 78, 80, 82</td>
<td>0 + 1/2 (7.6%)</td>
<td>1 + 4</td>
</tr>
<tr>
<td>Br</td>
<td>79, 81</td>
<td>3/2</td>
<td>4</td>
</tr>
<tr>
<td>I</td>
<td>127</td>
<td>5/2</td>
<td>6</td>
</tr>
</tbody>
</table>
The number of lines from the hyperfine interaction can be determined by the formula: \(2Nl + 1\). \(N\) is the number of equivalent nuclei and \(l\) is the spin. For example, an unpaired electron on a \(V^{4+}\) experiences \(l=7/2\) from the vanadium nucleus. We can see 8 lines from the EPR spectrum. When coupling to a single nucleus, each line has the same intensity. When coupling to more than one nucleus, the relative intensity of each line is determined by the number of interacting nuclei. For the most common \(l=1/2\) nuclei, the intensity of each line follows Pascal's triangle, which is shown below:

![Pascal's triangle](image_url)

Figure: Pascal's triangle
For example, for •CH₃, the radical’s signal is split to 2N+1= 2*3*1/2+1=4 lines, the ratio of each line’s intensity is 1:3:3:1. The spectrum looks like this:

![Simulated EPR spectrum of the •CH₃ radical.](http://en.wikipedia.org/wiki/File:EPR_methyl.png)
If an electron couples to several sets of nuclei, first we apply the coupling rule to the nearest nuclei, then we split each of those lines by the coupling them to the next nearest nuclei, and so on. For the methoxymethyl radical, H₂C(OCH₃), there are \((2\times2\times1/2+1)(2\times3\times1/2+1)=12\) lines in the spectrum, the spectrum looks like this:

![Simulated EPR spectrum of the H₂C(OCH₃) radical](http://en.wikipedia.org/wiki/File:EP...hoxymethyl.png)
For $I=1$, the relative intensities follow this triangle:

<table>
<thead>
<tr>
<th>$N$</th>
<th>Relative Intensities</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1</td>
</tr>
<tr>
<td>1</td>
<td>1 : 1 : 1</td>
</tr>
<tr>
<td>2</td>
<td>1 : 2 : 3 : 2 : 1</td>
</tr>
<tr>
<td>3</td>
<td>1 : 3 : 6 : 7 : 6 : 3 : 1</td>
</tr>
<tr>
<td>4</td>
<td>1 : 4 : 10 : 16 : 19 : 16 : 10 : 4 : 1</td>
</tr>
<tr>
<td>5</td>
<td>1 : 5 : 15 : 20 : 45 : 51 : 45 : 20 : 15 : 5 : 1</td>
</tr>
</tbody>
</table>

The EPR spectra have very different line shapes and characteristics depending on many factors, such as the interactions in the spin Hamiltonian, physical phase of samples, dynamic properties of molecules. To gain the information on structure and dynamics from experimental data, spectral simulations are heavily relied. People use simulation to study the dependencies of spectral features on the magnetic parameters, to predict the information we may get from experiments, or to extract accurate parameter from experimental spectra.
This splitting occurs due to hyperfine coupling (the EPR analogy to NMR’s J coupling) and further splits the fine structure (occurring from spin-orbit interaction and relativistic effects) of the spectra of atoms with unpaired electrons. Although hyperfine splitting applies to multiple spectroscopy techniques such as NMR, this splitting is essential and most relevant in the utilization of electron paramagnetic resonance (EPR) spectroscopy.
Hyperfine Splitting is utilized in EPR spectroscopy to provide information about a molecule, most often radicals. The number and identity of nuclei can be determined, as well as the distance of a nucleus from the unpaired electron in the molecule. Hyperfine coupling is caused by the interaction between the magnetic moments arising from the spins of both the nucleus and electrons in atoms. As shown in Figure, in a single electron system the electron with its own magnetic moment moves within the magnetic dipole field of the nucleus.

Figure: B is magnetic field, $\mu$ is dipole moment, 'N' refers to the nucleus, 'e' refers to the electron
This spin interaction in turn causes splitting of the fine structure of spectral lines into smaller components called hyperfine structure. Hyperfine structure is approximately 1000 times smaller than fine structure. Figure shows a comparison of fine structure with hyperfine structure splitting for hydrogen, though this is not to scale.

The total angular momentum of the atom is represented by $F$ with regards to hyperfine structure. This is found simply through the relation $F=J+I$ where $I$ is the ground state quantum number and $J$ refers to the energy levels of the system.
Results of Nuclear-Electron Interactions

These hyperfine interactions between dipoles are especially relevant in EPR. The spectra of EPR are derived from a change in the spin state of an electron. Without the additional energy levels arising from the interaction of the nuclear and electron magnetic moments, only one line would be observed for single electron spin systems. This process is known as hyperfine splitting (hyperfine coupling) and may be thought of as a Zeeman effect occurring due to the magnetic dipole moment of the nucleus inducing a magnetic field.

The coupling patterns due to hyperfine splitting are identical to that of NMR. The number of peaks resulting from hyperfine splitting of radicals may be predicted by the following equations where $M_i$ is the number of equivalent nuclei:

$\text{# of peaks} = M_i|I| + 1$ for atoms having one equivalent nuclei

$\text{# of peaks} = (2M_1I_1 + 1)(2M_2I_2 + 1)$ .... for atoms with multiple equivalent nuclei
For example, in the case of a methyl radical 4 lines would be observed in the EPR spectra. A methyl radical has 3 equivalent protons interacting with the unpaired electron, each with I=1/2 as their nuclear state yielding 4 peaks.

Figure: Approximate peaks resulting from hyperfine splitting between two inequivalent protons
The relative intensities of certain radicals can also be predicted. When \( I = 1/2 \) as in the case for \(^1\)H, \(^{19}\)F, and \(^{31}\)P, then the intensity of the lines produced follow Pascal's triangle. Using the methyl radical example, the 4 peaks would have relative intensities of 1:3:3:1. The following figures show the different splitting that results from interaction between equivalent versus non-equivalent protons.

It is important to note that the spacing between peaks is 'a', the hyperfine coupling constant. This constant is equivalent for both protons in the equivalent system but unequal for the inequivalent protons.
Hyperfine Coupling

Fine structure in EPR arises from hyperfine coupling between the electron and nuclear spin magnetic moments. The most prominent interaction is from Fermi contact by unpaired electrons with s character and the nucleus. A nucleus of spin n/2 give (n+1) lines with equal intensity. Furthermore, an electron can couple to n nuclei giving n+1 lines - the intensities of which follow a binomial distribution. The distance between these lines are measured in the change in magnetic field (gauss or tesla) and is called the Hyperfine Splitting Constant (A).

The g factor of paramagnetic electrons are different from the free electron due to coupling of the orbital angular momentum and the spin (spin-orbit coupling). The strength of the coupling is dependent on direction (anisotropic). For low viscosity solutions the effects of anisotropy are averaged out. However, in crystal EPR the sample molecules are oriented in a fixed direction and the anisotropy cannot be ignored. Every paramagnetic molecule has a principal axis system that is a set of unique axes that each have their own g values ($g_x$, $g_y$, and $g_z$) and hyperfine splitting constants.
Anisotropy causes the $g$ factor to be a second-rank tensor. The principle axis system must be selected such that the $g$-tensor $3 \times 3$ matrix can be diagonalized to three components $g_{xx}$, $g_{yy}$, and $g_{zz}$. For frozen powdered samples anisotropy can play a role depending on the system being studied.

<table>
<thead>
<tr>
<th>Type of Frozen Sample</th>
<th>$g$-value Relationship</th>
</tr>
</thead>
<tbody>
<tr>
<td>Isotropic</td>
<td>$g_x = g_y = g_z$</td>
</tr>
<tr>
<td>Axial</td>
<td>$g_x = g_y \neq g_z$</td>
</tr>
<tr>
<td>Rhombic</td>
<td>$g_x \neq g_y \neq g_z$</td>
</tr>
</tbody>
</table>
The hyperfine coupling constant ($\alpha$) is directly related to the distance between peaks in a spectrum and its magnitude indicates the extent of delocalization of the unpaired electron over the molecule. This constant may also be calculated. The following equation shows the total energy related to electron transitions in EPR.

$$
\Delta E = g_e \mu_e M_s B + \sum \frac{g_N \mu_N}{\mu_i} M_i (1 - \sigma_i) + \sum \alpha_i M_s M_i
$$

The first two terms correspond to the Zeeman energy of the electron and the nucleus of the system, respectively. The third term $\alpha_i$ is the hyperfine coupling between the electron and nucleus where $\alpha$ is the hyperfine coupling constant. Figure shows splitting between energy levels and their dependence on magnetic field strength. In this figure, there are two resonances where frequency equals energy level splitting at magnetic field strengths of $B_1$ and $B_2$. 
Figure: Splitting between energy levels and their dependence on magnetic field strength

These parameters are essential in the derivation of the hyperfine coupling constant. By manipulating the total energy equation the following two relations may be derived.

\[
B_1 = \frac{h\nu - a/2}{g\mu_e}
\]

\[
B_2 = \frac{h\nu + a/2}{g\mu_e}
\]
From this, the hyperfine coupling constant ($\alpha$) may be derived where is the \textit{g-factor}.

\[ \Delta B = B_2 - B_1 \]
\[ = \frac{\hbar \nu + \alpha/2}{g\mu_e} - \frac{\hbar \nu - \alpha/2}{g\mu_e} \]

so solving for hyperfine coupling constant results in the following relationship:

\[ a = g\mu_e \Delta B \]
Electron-nuclei interactions have several mechanisms, the most prevalent being Fermi contact interaction and dipole interaction. Dipole interactions occur between the magnetic moments of the nucleus and electron as an electron moves around a nucleus. However, as an electron approaches a nucleus, it has a magnetic moment associated with it. As this magnetic moment moves very close to the nucleus, the magnetic field associated with that nucleus is no longer entirely dipolar. The resulting interaction of these magnetic moments while the electron and nucleus are in contact is radically different from the dipolar interaction of the electron when it is outside the nucleus. This non-dipolar interaction of a nucleus and electron spin in contact is the Fermi contact interaction. A comparison of this is shown in Figure. The sum of these interactions is the overall hyperfine coupling of the system.
Fermi contact interactions predominate with isotropic interactions, meaning sample orientation to the magnetic field does not affect the interaction. Due to the fact that this interaction only occurs when the electron is inside the nucleus, only electrons in the s orbital exhibit this kind of interaction. All other orbitals (p, d, f) contain a node at the nucleus and can never have an electron at that node. The hyperfine coupling constant in isotropic interactions is denoted 'a'.

Figure: Different electron-nuclei interactions resulting in hyperfine coupling
Dipole interactions predominate with anisotropic interactions, meaning sample orientation does change the interaction. These interactions depend on the distance between the electron and nuclei as well as the orbital shape. The typical scheme is shown in Figure.

![Figure: Interaction between two dipoles with radius 'r'](image)

Dipole interactions can allow for positioning paramagnetic species in solid lattices. The hyperfine coupling constant in isotropic interactions is denoted 'B'.
Further splitting may occur by the unpaired electron if the electron is subject to the influence of multiple sets of equivalent nuclei. This splitting is on the order of \(2nI+1\) and is known as **superhyperfine splitting**. As hyperfine structure splits fine structure into smaller components, superhyperfine structure further splits hyperfine structure. As a result, these interactions are extremely small but are useful as they can be used as direct evidence for covalency. The more covalent character a molecule exhibits, the more apparent its hyperfine splitting.

For example, in a CH\(_2\)OH radical, an EPR spectrum would show a triplet of doublets. The triplet would arise from the three protons, but superhyperfine splitting would cause these to split farther into doublets. This is due to the unpaired electron moving to the different nuclei but spending a different length of time on each equivalent proton. In the methanol radical example, the electron lingers the most on the CH\(_2\) protons but does move occasionally to the OH proton.
Spin Relaxation Mechanisms

The excess population of lower state over upper state for a single spin system is very small as we can calculate from the following example. With the temperature of 298K in a magnetic field of 3000G, $N_{\text{upper}}/N_{\text{lower}} = 0.9986$, which means the populations of the two energy levels are almost equal, yet the slight excess in the lower level leads to energy absorption. In order to maintain a population excess in the lower level, the electrons from the upper level give up the $h\nu$ energy to return to the lower level to satisfy the Maxwell–Boltzmann law. The process of this energy releasing is called spin relaxation process, of which there are two types, known as spin–lattice relaxation and spin–spin relaxation.
This implies interaction between the species with unpaired electrons, known as "spin system" and the surrounding molecules, known as "lattice". The energy is dissipated within the lattice as vibrational, rotational or translational energy. The spin lattice relaxation is characterized by a relaxation time $T_{le}$, which is the time for the spin system to lose $1/e$th of its excess energy. Rapid dissipation of energy (short $T_{le}$) is essential if the population difference of the spin states is to be maintained. Slow spin lattice relaxation, which is of frequent occurrence in systems containing free radicals, especially at low temperatures, can cause saturation of the spin system. This means that the population difference of the upper and lower spin states approaches zero, and EPR signal ceases.
Spin-spin relaxation or Cross relaxation, by which energy exchange happens between electrons in a higher energy spin state and nearby electrons or magnetic nuclei in a lower energy state, without transferring to the lattice. The spin–spin relaxation can be characterized by spin-spin relaxation time $T_{2e}$.

When both spin–spin and spin–lattice relaxations contribute to the EPR signal, the resonance line width ($\Delta B$) can be written as

$$\Delta B \propto \frac{1}{T_{1e}} + \frac{1}{T_{2e}}$$

From the equation, we can tell that when $T_{1e} > T_{2e}$, $\Delta B$ depends primarily on spin–spin interactions. Decreasing the spin-spin distance, which is the spin concentration, $T_{1e}$ will become very short, approximately below roughly $10^{-7}$ sec, thus the spin lattice relaxation will have a larger influence on the linewidth than spin-spin relaxation. In some cases, the EPR lines are broadened beyond detection. When a spin system is weakly coupled to the lattice, the system tends to have a long $T_{1e}$ and electrons do not have time to return to the ground state, as a result the population difference of the two levels tends to approach zero and the intensity of the EPR signal decreases. This effect, known as saturation, can be avoided by exposing the sample to low intensity microwave radiation. Systems with shorter $T_{1e}$ are more difficult to saturate.
Advantages and Disadvantages

EPR has many useful applications for paramagnetic samples. It very useful for studies of complex macromolecules - specifically in identifying unknown molecules within macromolecules (e.g. Fe-S clusters), and is also useful for quantification (e.g. spin relaxation). EPR is a very sensitive technique and is capable of providing useful data in volumes as low as 300μL and concentrations as low as 1 μM. Furthermore, EPR spectra can be readily taken in 15-20 minutes once the equipment is prepared.

Although EPR has high specificity - that specificity relies on unpaired electrons which might not be relevant to every system being studied. Most paramagnetic materials need temperatures as low as 20K for detection which can be an expensive constraint.
EPR is a very useful tool to study proteins with metal clusters, as proteins are usually in low concentration and volume. Just the ability of EPR to probe a metal site in an enzyme reveals information. For example, in [NiFe] hydrogenase there are many steps in the catalytic cycle where an iron atom is EPR silent and a nickel atom switches between EPR active and silent depending on the catalytic state. This, coupled with coordination information from the crystal structure, is strong evidence that the EPR silent iron must be low spin Fe(II) and the nickel cycles between Ni(I) and Ni(II) in the different catalytic states.

Also, it is very popular to spin label sites in a protein for exploration with EPR. Spin labeling usually takes advantage of the reactivity of protein thiol groups from cysteines. The most commonly used spin label is a nitroxyl radical bound to a larger heterocyclic ring. In principle this allows previously EPR silent regions to be explored. By using complex pulsed EPR techniques, such as double electron electron resonance, the distances between spin labels (or natural paramagnetic sites) can be determined - this is especially useful when crystallographic structures are unavailable.

Recently, EPR spectroscopy has emerged as a powerful tool to study the structure and dynamics of biological macromolecules such as proteins, protein aggregates, RNA and DNA. It is used in combination with molecular modelling to study complex systems such as soluble proteins, membrane proteins and protein aggregates like amyloid fibrils and oligomers.

https://www.ias.ac.in/article/fulltext/reso/020/11/1017-1032
Further Suggested Reading

- https://sites.cns.utexas.edu/epr_facility/what-epr
- https://pubs.acs.org/doi/abs/10.1021/ef00016a015
- https://www.ncbi.nlm.nih.gov/pmc/articles/PMC3839053/
CHAPTER 3

Electron Paramagnetic Resonance (EPR) Spectroscopy

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1. Introduction

Electron paramagnetic resonance (EPR) spectroscopy, also called electron spin resonance, is a technique that is used to study chemical species with unpaired electrons. EPR spectroscopy plays an important role in the understanding of organic and inorganic radicals, transition metal complexes, and some biomolecules.

An electron is a negatively charged particle with certain mass; it mainly has two kinds of movements. The first one is spinning around the nucleus, which brings orbital magnetic
moment. The other is spinning around its own axis, which brings spin magnetic moment. Like most spectroscopic techniques, EPR spectrometers measure the absorption of electromagnetic radiation.

The EPR spectrum of a free radical is the simplest of all forms of spectroscopy. If an external magnetic field is not present, the two electron spin states (spin up and spin down) are degenerate. The degeneracy of the electron spin states characterized by the quantum number, $m_s = \pm 1/2$, is lifted by the use of a magnetic field. Transitions between the electron spin levels are induced by radiation at the matching frequency. When a magnetic field is induced, atoms with unpaired electrons spin either in the same direction (spin up) or in the opposite direction (spin down) of the applied field. These two possible alignments with different energies are no longer degenerate. The alignments are directly proportional to the applied magnetic field strength. This is called the Zeeman effect. An unpaired electron interacts with its environment, and the details of EPR spectra depend on the nature of those interactions. The readings can provide information on structural and dynamic information, even from the chemical or physical process, without influencing the process itself. The energy associated with the transition is expressed in terms of the applied magnetic field $B$, the electron spin $g$-factor $g$, and the constant $\mu_B$, which is called the Bohr magneton.

The EPR technique has been widely used to study the structure and function of biological membranes.

Biological membranes play a vital role in the cell structure and function. Mass and information transport through the membrane are the most important biological functions, whereas the membranes divide the cell into several different compartments. Researches in the past decades have shown that membranes consist of a laterally heterogeneous lipid bilayer with a large number of embedded protein molecules. The bilayer is heterogeneous either in the way of molecular assembly or in the way of the assembly of molecular aggregates. The molecules and the super molecular aggregates thus interact with each other by different interaction forces and exhibit a variety of characteristics in the transport. The elucidation of the structure and function of the biological membrane has been recognized as a formidable task. Despite its complexity, the EPR technique is considered as one of the most important techniques, both experimentally and biologically.

Unlike biological membranes, the application of the EPR technique to investigate the synthetic polymeric membranes is very rare and none can be found for ceramic membranes. This is very surprising, considering the fact that the biomimetic membrane such as aquaporin membrane currently occupies the center position in the development of novel separation membranes.

It is attempted in this article to review the EPR applications for the study of synthetic polymeric membranes. The fundamentals of the EPR technique that are outlined before
some examples of EPR applications in the synthetic polymeric membranes are shown. Then, the EPR works that have potential in the future investigation of separation membranes are collected from the literature and the problems that should be addressed for the wider applications of the EPR technique are shown.

2. Fundamentals of EPR

2.1 Principle of Electron Paramagnetic Resonance

Magnetic moment of the molecule is primarily contributed by unpaired electron (Fig. 3.1). By increasing the external magnetic field, the gap between two energy states is widened until it matches the energy of the microwaves, as represented by the double arrow in the diagram above. At this point the unpaired electrons can move between their two spin states. Since there are typically more electrons in the lower state, due to the Maxwell–Boltzmann distribution, there is a net absorption of energy, and it is this absorption that is monitored and converted into a spectrum (see Fig. 3.2). The upper spectrum below is the simulated absorption for a system of free electrons in a varying magnetic field. The lower spectrum is the first derivative of the absorption spectrum. The latter is the most common way to record and publish EPR spectra.

If we are dealing with systems with a single spin like this example, then EPR would always consist of just one line and would have little value as an investigative tool, but several factors influence the effective value of $g$ in different settings. Since the source of an EPR spectrum is a change in an electron’s spin state, it might be thought that all EPR spectra for a single electron spin would consist of one line. However, the interaction of an unpaired electron, by way of its magnetic moment with nearby nuclear spins, results in additional allowed energy states and, in turn, multilined spectra. In such cases, the spacing between the EPR spectral lines indicates the degree of interaction between the

![Figure 3.1](image)

*Figure 3.1*

Energy levels for an electron spin ($m_s = \pm 1/2$) in an applied magnetic field $B_0$ [1].
unpaired electron and the perturbing nuclei. The hyperfine coupling constant of a nucleus is directly related to the spectral line spacing and, in the simplest cases, is essentially the spacing.

Fundamentally EPR is similar to the more widely familiar method of nuclear magnetic resonance (NMR) spectroscopy, with several important distinctions. Although both spectroscopies deal with the interaction of electromagnetic radiation with magnetic moments of particles, there are many differences between the two spectroscopies:

1. EPR focuses on the interactions between an external magnetic field and the unpaired electrons of whatever system it is localized to, as opposed to the nuclei of individual atoms.
2. The electromagnetic radiation used in NMR typically is confined to the radio frequency range between 300 and 1000 MHz, whereas EPR is typically performed using microwaves in the 3–400 GHz range.
3. In EPR, the frequency is typically held constant, whereas the magnetic field strength is varied. This is the reverse of how NMR experiments are typically performed, where the magnetic field is held constant while the radio frequency is varied.
4. Due to the short relaxation times of electron spins in comparison to nuclei, EPR experiments must often be performed at very low temperatures, often below 10K, and sometimes as low as 2K. This typically requires the use of liquid helium as a coolant.
5. EPR spectroscopy is inherently roughly 1000 times more sensitive than NMR spectroscopy due to the higher frequency of electromagnetic radiation used in EPR in comparison to NMR.
EPR permits observation of any substance having unpaired electrons. Some examples of substances that exhibit this quality are as follows:

1. Atoms or ions having partially filled inner electron shells that are all of the transition elements of the iron series, rare earth’s and platinum series.
2. Molecules having an odd number of electrons in their outer shells (e.g., NO or ClO₂).
3. Molecules with an even number of electrons in their outer shells but with a resultant magnetic moment (e.g., O₂).
4. Free radicals, which are naturally or artificially produced.
5. Conduction electrons in metals and acceptors and donors in semiconductors.
6. Modified crystal structure and defects in crystals, e.g., color centers.

EPR study is affected by the degree of detail desired and by the type of problem investigated. It is sensitive to the local environment.

### 2.2 Electron Spin and Magnetic Moment

As discussed earlier, an electron is a negatively charged particle with certain mass and has mainly two kinds of movements. The first one is spinning around the nucleus, which brings orbital magnetic moment, and the other is spinning around own axis, which brings spin magnetic moment. Magnetic field of the molecule is primarily contributed by unpaired electron’s spin magnetic moment, which is given by,

\[ M_S = \sqrt{S(S+1)} \frac{\hbar}{2\pi} \]  

(3.1)

\( M_S \) is the total spin angular momentum, \( S \) is the spin quantum number, and \( \hbar \) is Planck’s constant. In the \( z \) direction, the component of the total spin angular momentum can only assume two values:

\[ M_{Sz} = m_s \frac{\hbar}{2\pi} \]  

(3.2)

the term \( m_s \) has \( 2S + 1 \) different values: \( +S, (S - 1), (S - 2), \ldots, -S \). For single unpaired electron, only two possible values for \( m_s \) are \( +1/2 \) and \( -1/2 \).

The magnetic moment, \( \mu_e \) is directly proportional to the spin angular momentum and one may therefore write

\[ \mu_e = -g_e \mu_B M_S \]  

(3.3)

The appearance of negative sign is because the magnetic moment of electron is collinear but antiparallel to the spin itself. The term \( (g_e \mu_B) \) is the magnetogyric ratio. The factor \( g_e \) is known as the free electron \( g \)-factor with a value of 2.002 319 304 386 (one of the most
accurately known physical constants). The Bohr magneton, $\mu_B$, is the magnetic moment for one unit of quantum mechanical angular momentum:

$$\mu_B = \frac{e\hbar}{4\pi m_e}$$

(3.4)

where $e$ is the electron charge, $m_e$ is the electron mass.

This magnetic moment interacts with the applied magnetic field. The interaction between the magnetic moment ($\mu_e$) and the field ($B$) is described by

$$E = -\mu_e B$$

(3.5)

For single unpaired electron, there will be two possible energy states, this effect is called Zeeman splitting.

$$E_{+\frac{1}{2}} = \frac{1}{2} g\mu_B B$$

(3.6)

$$E_{-\frac{1}{2}} = -\frac{1}{2} g\mu_B B$$

(3.7)

In the absence of external magnetic field, $E_{+1/2} = E_{-1/2} = 0$.

In the presence of external magnetic field, as illustrated in Fig. 3.1, with the absorption of radiation, the difference between the two energy states can be written as

$$\Delta E = h\nu = g\mu_B B$$

(3.8)

With the intensity of the applied magnetic field increasing, the energy difference between the energy levels widens until it matches with the microwave radiation and results in absorption of photons.

### 2.3 Hyperfine Coupling

Since the source of an EPR spectrum is a change in an electron’s spin state, it might be thought that all EPR spectra for a single electron spin would consist of one line. However, the interaction of an unpaired electron, by way of its magnetic moment, with nearby nuclear spins, results in additional allowed energy states and, in turn, multilined spectra. In such cases, the spacing between the EPR spectral lines indicates the degree of interaction between the unpaired electron and the perturbing nuclei. The hyperfine coupling constant of a nucleus is directly related to the spectral line spacing and, in the simplest cases, is essentially the spacing itself.

### 2.4 Block Diagram of EPR Spectrometer

Fig. 3.3 shows a block diagram for a typical EPR spectrometer. The radiation source usually used is called a klystron. Klystrons are vacuum tubes known to be stable
high-power microwave sources, which have low-noise characteristics and thus give high sensitivity. A majority of EPR spectrometers operate at approximately 9.5 GHz, which corresponds to about 32 mm. The radiation may be incident on the sample continuously [i.e., continuous wave (cw)] or pulsed. The sample is placed in a resonant cavity, which admits microwaves through an iris. The cavity is located in the middle of an electromagnet and helps to amplify the weak signals from the sample. Numerous types of solid-state diodes are sensitive to microwave energy and absorption lines then can be detected when the separation of the energy levels is equal or very close to the frequency of the incident microwave photons. In practice, most of the external components, such as the source and detector, are contained within a microwave bridge control. Additionally, other components, such as an attenuator, field modulator, and amplifier, are also included to enhance the performance of the instrument.

2.5 Spin-Labeling Method

Most chemical and biological samples of interest for EPR spectroscopy lack an inherent stable unpaired electron, the majority of EPR methods rely on the usage of spin-labeling reagents. The radical so introduced is often called a spin label or a spin probe. It is invariably a nitroxide radical, which exhibits a three-line hyperfine structure whose peak shape, splitting, etc., depend on the radical’s environments. The nitroxide label is a monitor of motion. The shape of the EPR signal depends also on the orientation of the magnetic field relative to the axis of the radical. Thus, the spin label method is useful to study the environment of radical, which is the structure of the polymer at a molecular level.
Commonly, nitroxides such as derivatives of TEMPO (2,2,6,6-tetramethyl-1-piperidinyloxy) are used as they offer high stability of the unpaired electron and exceptional EPR sensitivity combined with facile and versatile moieties for binding to the sample through chemical reactions itself. Fig. 3.4 shows the EPR spectra of TEMPO solution in water (0.02 wt%). The spectra consist of three symmetric peaks since the NO\(^*\) radical of TEMPO (or with 5-, 12-, and 16-doxylstearic acid derivatives) is freely mobile in the solution. The spectra are isotropic (symmetric) and the value of Hamiltonian parameter, the factor \(g_e\) is known as the free electron \(g\)-factor with a value of 2.002 319 304 386 (one of the most accurately known physical constants) and \(|A|\) (distance between two peaks) is 17 G. All three peaks are almost equal in height and symmetric.

Interactions of an unpaired electron with its environment influence the shape of an EPR spectral line. The shape of curves and other properties of the EPR spectra gives the clue for analysis.

3. **EPR Applications for the Synthetic Polymeric Membranes**

3.1 **EPR Applications at the University of Ottawa**

Khulbe and Matsuura [4] wrote a review in which they discussed the characterization of synthetic membranes by EPR.
The radicals were detected in the polymeric material from which membranes are fabricated and the number of radicals depended on the conditions in which the membranes were fabricated and the environment to which the membranes were exposed. Polymers themselves contain paramagnetic free radicals. It is possible that these radicals may take part in the transportation of gases through the membrane. It is observed that these radicals are affected reversibly with gases (CO₂ and CH₄). Khulbe et al. [5] reported that polyphenylene oxide (PPO) radicals are present in PPO powder, and the membranes prepared from PPO contain free radicals that are affected by the conditions of the environment. It was reported that the number of spins/g in membranes is higher than in the PPO powder and it also depends on the characteristics of solvents used for membrane preparation. Generally, the number of spins/g in vacuum is less than in the air. However, no definite conclusion could be drawn due to small quantity of spins (10¹⁴ spins/g). It was noticed that in the presence of N₂ the number of spins/g (concentration) was more than that in the presence of O₂. On the contrary, the number of spins/g was higher in the presence of CH₄ than CO₂. The permeation rates through the membrane of CO₂ and O₂ are usually higher than CH₄ and N₂, respectively. This type of behavior also was observed with sulfonated and brominated PPO membranes [4].

Incorporation of the spin label TEMPO was also attempted by Khulbe et al. [6]. Dense homogeneous PPO membranes were prepared by casting a solution, which consisted of PPO, TEMPO (spin probe), and 1,1,2-trichloroethylene solvent. The solvent was evaporated at 22, 4, and −10°C. Membranes were subjected to EPR spectroscopic study as well as to the permeability measurement of various gases, including O₂, N₂, CO₂, and CH₄. It was observed that the intensity of the spin probe decreased with the decrease of temperature used for the preparation of the membrane. The intensity of the spin probe was almost at zero level for the membrane prepared at −10°C in comparison with the EPR signal intensity of the other two membranes prepared at higher temperatures. It could be due to high crystallinity state in the membrane prepared at −10°C or some level of molecular ordering. Authors concluded that

1. The intensity of the spin probe in the PPO membrane depends on the temperature of solvent evaporation during dense membrane preparation.
2. The morphology of the surface on the membrane depends on the temperature used for the preparation of the membrane.
3. Generally, the permeation rate of gases (especially with CO₂ and CH₄) increases with the decrease in the temperature used for the preparation of membrane. It could be possible that Langmuir sites are most favorable for the CH₄ and N₂ permeation in PPO membrane. It could be possible that Henry sites are good for selectivity.

Gumi et al. [7] studied activated composite membranes by EPR and reported that EPR is a useful tool for the characterization of activated composite membranes.
Another example of the incorporation of spin label is the work by Khulbe et al. [3] who prepared dense membranes from poly(phenylene oxide) (PPO) by blending spin probes (TEMPO, 5-, 12-, and 16-doxylstearic acid) in the casting solution. It was noticed that the shape and size of the probe influence the EPR spectra of the NO* radical in the PPO membrane. Unexpectedly, from the shape of the EPR signal it was noticed that the NO* radical of TEMPO in PPO membrane was more mobile than in water media. However, the motion of the NO* radical of 16-doxylstearic acid was higher than that of NO* radical of 5- and 12-doxylstearic acid when the radicals were in the PPO membrane. This could be due to the inductive effect from COOH group. The Hamiltonian parameters of the EPR signal indicated that all the probes were not randomly distributed in the PPO membrane, but some probes were distributed in the polymer in orderly fashion.

Khulbe et al. [8] studied the structure of the skin layer of asymmetric cellulose acetate (CA) RO membranes with TEMPO probe. It was observed that the mobility of TEMPO in the asymmetric membrane shrunk at 90°C was the same as TEMPO in a dense homogeneous membrane prepared from the same casting solution. Authors reported the following conclusions

1. The pore sizes of the asymmetric membranes are larger when they were shrunk at lower temperatures
2. The space in the polymer network (the origin of the network pore) in the dense film was smaller when no swelling agent is added to the casting solution
3. The space in the polymer network in the dense film was smaller when the membrane was dry

In another study, Khulbe et al. [9] used EPR spectroscopy as a method to study membrane fouling during ultrafiltration (UF). Bovine serum albumin (BSA) and polyethylene oxide, with and without TEMPO (spin probe), solutions in water were used as the feed in the UF experiments. Asymmetric membranes were prepared by phase inversion technique using casting solutions of polyethersulfone (PES) in n-methyl pyrrolidone. Polyvinyl pyrrolidone was added as a nonsolvent additive. The following conclusions were reported.

1. Deposition of BSA on the surface and inside the pore during UF is in a specific orientation (manner). However, the orientation of BSA molecule on the surface is different from that of the BSA molecule inside the pore.
2. The packing density of BSA molecules inside the pore depends on the particular pore size and feed pressure. At higher feed pressure, the denser packing moves toward smaller pore size.
3. Fouling depends on the structure of solute.

EPR spectroscopy technique was also used to study CA membranes for reverse osmosis (RO) and PES membranes for UF [10]. TEMPO was used as a spin probe that was
brought into the membranes by immersing the membranes into solutions involving TEMPO, or by blending TEMPO into membrane casting solutions. The following conclusions were reported:

1. EPR technique can be used to study the structure and the transport of RO and UF membranes.
2. Water may flow through the pores of PES membranes. The sizes of pores are those of UF membranes. Unlike CA, the polymer matrix of PES membrane is a little swollen or not at all swollen by water and continuous channels through which water flows cannot be formed. In CA, spaces in water swollen polymer matrix were the primary provider of continuous flow channels that contribute to the separation of salt and small organic molecules. In the absence of such water channels, PES membranes cannot act as RO membranes.

Khulbe et al. [11] reported the EPR study on the structure and transport of asymmetric aromatic polyamide membranes. TEMPO was used as a spin probe that was brought into the membrane by (a) immersion of the membranes in aqueous TEMPO solutions, (b) RO experiments with feed solutions involving TEMPO, or (c) blending TEMPO in casting solutions. The membranes were tested for the separation of sodium chloride and TEMPO from water by RO. It was concluded that aromatic polyamide membranes contain water channels in the polymer matrix like CA membranes. A comparison was made with other RO membranes (CA) and UF membranes (PES). It was suggested that the EPR technique can be used to study the structure of UF and RO membranes. The presence of water channels in the polymer matrix seems indispensable for the RO membrane.

### 3.2 Applications of EPR to Study Fouling of RO and UF Membranes

Membrane fouling and aging were studied by the other groups using EPR technique. Oppenheim et al. [12] spin-labeled hen egg lysozyme (HEL) with 3-maleimido-proxy at two positions of macromolecule. HEL solution was ultrafiltered in a cross-flow UF apparatus for 2 h using polysulfone UF membrane of molecular weight cutoff (MWCO) = 10 kDa. Then, spin-labeled HEL in saline buffer solution and on the UF membrane were subjected to EPR analysis. Figs. 3.5 and 3.6 show the EPR signals obtained from HEL in the buffer solution and HEL in the UF membrane, respectively. The peaks indicated in Fig. 3.6 by arrows were ascribed by the authors to the spin—spin interaction between two spin labels of HELs confined in narrow pore channels. When HEL was ultrafiltered by UF membrane of MWCO = 30 kDa, the EPR signal was similar to that of HEL in the buffer solution, indicating the pores of the latter membrane (MWCO = 30 kDa) were not blocked by HELs.

RO and UF membranes are often cleaned chemically by contacting the membranes with hypochlorite solution. It has long been suggested that degradation of polymer takes place
during the membrane cleaning due to radical formation [13]. To confirm this hypothesis Oliveira et al. studied, using EPR technique, the aging of polyamide thin film composite membrane during the chemical cleaning by hypochlorite solution changing the hypochlorite concentration as well as pH [14].

**Figure 3.5**
Electron paramagnetic resonance signal from the hen egg lysozyme in buffer solution [12].

**Figure 3.6**
Electron paramagnetic resonance signal from the hen egg lysozyme in the UF membrane (MWCO 10 kDa) pore [12].
Dow Filmtech NF 270 membrane was immersed in bleach solution (NaClO₃) before the membrane was dried and transferred into a quartz tube for EPR observation. The intensity of the EPR signal has increased with an increase of bleach concentration as shown in Fig. 3.7, whereas the radical formation was suppressed by increasing pH (Fig. 3.8). Unfortunately, the radical species could not be identified due to the absence of the hyperfine structure.

They have also studied the effect of the membrane exposure to the sunlight on the radical formation and the radical formation during the ultraviolet (UV) membrane surface grafting and confirmed that the membrane degradation occurred under an excessive UV irradiation.

4. Other Examples of EPR Applications

4.1 Aging of Proton Exchange Membranes

The degradation of proton exchange membranes (PEMs) is an important subject in the fuel cell application. As a typical PEM Nafion was chosen and its degradation mechanism was studied by EPR when Nafion was neutralized by Cu(II), Fe(II), and Fe(III) ions [15].

When Nafion was neutralized by FeSO₄ and irradiated by UV, the signal from ROCF₂CF₂ radical was detected and its intensity increased with the UV irradiation time (Fig. 3.9).

Remarkably, the signal was also observed even before the UV irradiation, indicating radical formation in the presence of Fe(II) without UV irradiation. At the same time the formation of Fe(III) was detected.
Figure 3.8
Electron paramagnetic resonance spectra after the membrane was immersed in 50 v/v% bleach solution at (a) pH = 8 and (b) pH = 9 [14].

Figure 3.9
Electron paramagnetic resonance signal for ROCF₂CF₂· radical when neutralized by Fe(II) [15].
Thus, the radical formation and polymer degradation are possible in the presence of metal ions such as Cu(II), Fe(II), and Fe(III) even without UV irradiation.

4.2 Study of Carbon Nanotubes

Much attention has been paid to carbon nanotubes (CNTs) to apply them for separation membranes due to their extraordinarily high permeability for water and gas. Many attempts have also been made to incorporate them in the mixed matrix membranes (MMMs) [16]. The study of CNTs by EPR was conducted even before the announcement of the unusual permeation characteristics of CNTs by Hinds et al. [17].

Multiwalled CNTs were embedded in styrene-polyisoprene-polystyrene (SIS) block copolymer and its EPR spectra were recorded [18]. The resonance spectrum of SIS-CNTs composite is featured by a strong and symmetric peak at $g = 2.06$ and the resonance line width of $102 \text{ G}$, which was ascribed to the strongly interacting localized and itinerant electrons, in the so-called bottleneck state.

The double integral of the resonance line called $S$ is proportional to the susceptibility. When $S$ is plotted versus temperature (Fig. 3.10), $S$ depends only weakly on temperature when the CNT content in the composite is low, but $S$ depends strongly on temperature when the CNT content is high. Since susceptibility $S$ of localized electron is temperature dependent, whereas $S$ of delocalized electron is temperature independent, Fig. 3.10 means that the amount of localized electron is very small when the CNT content is low. These localized electrons were most likely those of Fe$^{3+} \text{ ions}$ in the residual catalyst of CNT synthesis. As the CNT loading increases, the amount of

![Figure 3.10](image)

**Figure 3.10**

Temperature dependence of $S$ [18].
localized electrons (paramagnetic defects) increases and so does the temperature dependency. This means these paramagnetic defects are localized either within CNTs themselves or at the CNTs—polymer interface.

Another study on CNTs was done by Rao et al. [19].

Double walled carbon nanotubes of 0.45 nm average diameter were embedded in VP 15 molecular sieve (zeolite) nanochannels and subjected to EPR at temperatures 4.2, 20, 40, 60, and 75K. From Fig. 3.11, for all temperatures a symmetric EPR signal is observed at \( g_c \approx 2.0028 \) with a corresponding density \( \approx 10^{19} \text{g}^{-1} \).

Generally, for single walled carbon nanotubes (SWCNTs) and MWCNTs of much larger diameter (more than 1 nm) different types of EPR signals are observed, i.e., (1) signal centered at \( g_c = 2.0 \) coming from the residual metal catalytic particles, (2) \( g_c = 2.07 \) coming from the conduction electron spin resonance, and (3) \( g_c = 2.00 \) coming from localized electron spins. Therefore, Fig. 3.11 excludes the possibility of the presence of conduction electrons. The electrons are localized in the defect on the CNTs.

![Electron paramagnetic resonance signal of carbon nanotubes embedded in zeolite at different temperatures](image)

**Figure 3.11**
Electron paramagnetic resonance signal of carbon nanotubes embedded in zeolite at different temperatures [19].
4.3 Metal Organic Frameworks

Much attention is also paid to metal organic frameworks (MOFs) due to its unique structures that allow strong adsorption of gaseous molecules [20]. They are also embedded in polymeric membrane to form MMMs for gas and liquid separation [21].

MOF expands in their crystalline structure when guest molecules are adsorbed in it, whereas it shrinks when the molecules are desorbed, a phenomena known as “breathing.” It was confirmed by EPR that similar structural change takes place when temperature changes from high (HT) to low (LT) and vice versa. Cr(III)-doped aluminum-based MIL-53 was synthesized where the main metal ion is Al (99%), whereas the rest of 1% is Cr. The sample was further calcinated and evacuated to remove water and residual organic acid and it was called MIL-53(Al/Cr)deh, where deh means dehydration.

The Q-band EPR spectra of MIL-53(Al/Cr)deh taken at different temperatures are shown in Fig. 3.12.

At 295K (Fig. 3.12(a,b)), three singularities ($\theta = 0$ degree, 42 degree, and 90 degree) of the central $M_S = -1/2 \leftrightarrow 1/2$ transition appear between 1170 and 1320 mT. Furthermore, two single $\theta = 90$ degree edge singularities of the $M_S = \pm 3/2 \leftrightarrow \pm 1/2$ transitions are observed at 940 and 1540 mT without splitting, indicating an axially symmetric tensor ($E \approx 0$). Then, the ratio of spin Hamiltonian parameters $E/D$ becomes nearly equal to

![Figure 3.12](image-url)

Electron paramagnetic resonance spectra of MIL-53(Al/Cr)deh at (a) experimental, (b) simulated at 295K, (c) experimental, and (d) simulated at 5K [21].
zero, hence these signals are assigned to CrO$_4$(OH)$_2$ octahedral (Fig. 3.13(a)) in the HT phase of MIL-53(Al/Cr)deh.

On the other hand, at a lower temperature of 5K, the Q-band spectrum transformed to rhombic nature (Fig. 3.12(c,d)) and the signals at 940 and 1540 mT disappeared, which means the ratio of spin Hamiltonian parameters $E/D$ is no longer zero (by simulation $E/D$ ratio was found to be 0.236), suggesting the lowering in the symmetry of CrO$_4$(OH)$_2$ octahedrons (see Fig. 3.13(b)).

It was further proposed that high to low temperature transition occurs at temperatures between 150 and 60K, whereas the transformation from low to high transition occurs at the temperatures between 330 and 375K, indicating the large thermal hysteresis. As well about 20% of the material does not undergo the transition high to low temperature.

### 4.4 State of Interfacial Water

Two polypeptides, 26-residue polypeptide (n3) and 14-mer long proline model peptide (PPm3), were spin labeled and dissolved in vitrified solvent (concentrated aqueous sucrose or glycerol solution) or confined in two mesoporous silica materials, SBA15a

![Figure 3.13](image)

Schematic presentation of MIL-53(Al/Cr)deh structure, (a) 295K, (b) 5K [21].
and SBA15b, with pore diameters of 7.6 and 6.1 nm, respectively. Then, they were subjected to several EPR studies including double electron resonance, electron spin echo, and electron spin echo envelope modulation (ESEEM). As well, H2O was sometimes changed to D2O [22]. The parameter π(D2O) measured by ESEEM shows the accessibility of water, especially D2O, within the van der Waals contact distance of c. 0.35 nm from the spin label.

As shown in Table 3.1, π parameter does not change in the vitrified solvent or in the pore of SBA 15a and SBA 15b. Only when the peptide PPm3 was in the vitrified solvent containing 40% glycerol, the accessibility was nearly doubled.

On the other hand, the parameter \( C_{ex} \), which indicates the density of water (D2O in this case) within the range of 2 nm of the spin label is remarkably different, depending on the confinement in the nanopore. The values for both n3 and PPm3 are in the order of SBA 15b > SBA 15a > vitrified solvent and remarkably high when the polypeptides are confined in SBA 15b with the nanopores of the smaller diameter. Thus, this result confirms that there is density profile in the vicinity of the spin-labeled polypeptide, indicating the presence of special water near polypeptides that represent proteins, so-called “biological surface water.” The importance of such water for sustaining “life” is well recognized.

The presence of special water in RO membrane, most likely in the membrane pore, has long been recognized by differential scanning calorimetric (DSC) experiments [23]. Thus, EPR can possibly be a powerful tool to sense the presence of special interfacial water in the membrane pore.

**5. Conclusions**

It was shown that the EPR technique is a powerful tool to study the synthetic polymeric membranes by showing:

1) Radicals are present in the synthetic polymeric membrane.

| Table 3.1: π Parameter and density (\( C_{ex} \)) profile in the vicinity of spin-labeled polypeptide. |
|---------------------------------------------------------------|-----------------|-----------------|
| 26-residue polypeptide (n3) in SBA 15a                        | 0.185           | 24.2            |
| n3 in SBA 15b                                                | 0.156           | 42.3            |
| n3 in 40% sucrose solution                                   | 0.142           | 12.8            |
| 14-mer long proline model                                   | 0.215           | 28.6            |
| peptide (PPm3) in SBA 15a                                   | 0.479           | 23.0            |
| PPm3 in SBA 15b                                              | 0.132           | 60.9            |
| PPm3 in 40% glycerol solution                                |                |                 |
1.1) The concentration of radicals is different depending on the conditions by which membranes are fabricated. The macromolecular radicals in the membrane may lead to the degradation of polymer by radical reactions.

1.2) The radical concentration increases during the chemical cleaning of the membrane, leading to polymer degradation. The radical concentration also increases by exposure to sunlight and during the surface modification by UV grafting.

2) The spin-labeling technique is a powerful tool to characterize the membrane morphology. In particular,

2.1) The order in the macromolecular alignment in the membrane can be detected at the molecular level, which might affect the membrane selectivity in gas separation.

2.2) The difference in the nature of the pores in RO and UF membranes can be identified. Water passes through the swollen intersegmental space (network pores) in the skin layer of the CA RO membrane, whereas in the PES UF membrane water flows through pores formed between the polymer aggregates (aggregate pores).

2.3) The network pores of the CA membranes shrink when the membrane is annealed.

2.4) EPR technique confirms that membrane fouling takes place by protein molecules that are densely packed in the membrane pores.

It was shown by some other examples that

1) Radicals were found in the Nafion PEMs when its sulfonic group was partially neutralized by Cu or Fe ions, causing the degradation of the PEMs.

2) It was found that the electron was highly localized in the CNT itself, in the space between CNT and polymer matrix, or in the defect of CNTs.

3) Hysteresis was observed between the expansion of MOF at the HT and shrinkage at the LT, which resembles the breathing of MOF that occurs by adsorption and desorption of guest molecules.

4) The density profile was detected near protein molecules that are confined in nano-channels. This proves the presence of the interfacial water at the protein/water interface.

It should also be noted that the EPR applications for the synthetic polymeric membranes, although they can give some insights into the membrane structure and performance, all of the currently available works lack precise analysis of the hyperfine structures of the EPR signals.

On the other hand, in the other works, the hyperfine structures of EPR signals were analyzed more rigorously, giving details of the EPR signal sources. Unfortunately, however, it is very difficult to understand how the EPR parameters can be interpreted due to the complexity of the EPR theory.
As well, EPR technique has the following drawbacks compared to the other characterization techniques.

1) It is impossible to obtain two-dimensional (2D) or three-dimensional (3D) images of the membrane surface (and the cross-section) unlike scanning electron microscope, transmission electron microscope, and atomic force microscope.

2) Currently, it is impossible to investigate the surface of the membrane separately from the bulk, unlike FTIR-ATR, XPS, EDX, and contact angle measurement.

3) Hence, the data are affected by the bulk structures under the top surface layer that governs the performance of the asymmetric membrane, similar to XRD, DSC, TGA, and measurement of mechanical strength.

Thus, the complication involved in the theoretical interpretation of EPR, absence of 2D and 3D images taken by the EPR technique and difficulty in the surface observation is now hampering the wider usage of the EPR technique to investigate the synthetic polymeric membrane despite its enormous potential to reveal the details of the membrane structure.

References


Principles and applications of EPR spectroscopy in the chemical sciences

Maxie M. Roessler \textsuperscript{a,b}\textsuperscript{*} and Enrico Salvadori \textsuperscript{a,b}\textsuperscript{*}

Electron spins permeate every aspect of science and influence numerous chemical processes: they underpin transition metal chemistry and biochemistry, mediate photosynthesis and photovoltaics and are paramount in the field of quantum information, to name but a few. Electron paramagnetic resonance (EPR) spectroscopy detects unpaired electrons and provides detailed information on structure and bonding of paramagnetic species. In this tutorial review, aimed at non-specialists, we provide a theoretical framework and examples to illustrate the vast scope of the technique in chemical research. Case studies were chosen to exemplify systematically the different interactions that characterize a paramagnetic centre and to illustrate how EPR spectroscopy may be used to derive chemical information.

Key learning points
(1) An understanding of the physical principles in EPR spectroscopy is fundamental to deriving any information from EPR spectra beyond simple detection of the signals.
(2) EPR spectroscopy can tackle many different chemical questions, ranging from identification of the paramagnetic centre, to detailed information on structure and bonding.
(3) Many continuous-wave and pulse EPR experiments exist. Pulse EPR experiments are frequently designed to single out a particular magnetic interaction (e.g. hyperfine coupling, dipolar coupling) and choosing the right experiment is often key to success.
(4) Visual inspection of EPR spectra may lead to good estimates of parameters (e.g. g values, hyperfine coupling constants or even zero-field splitting), but simulation is usually required to interpret spectra fully.

1 Introduction
Since Yevgeny Zavoisky recorded the first EPR spectra of copper and manganese over 70 years ago on a home-built spectrometer, EPR spectroscopy has made seminal contributions in all areas of chemistry, as well as in biology, physics and materials science. However, to many chemists EPR spectroscopy is not a very accessible field. This is perhaps because most EPR literature is aimed at experienced researchers already working in the field. A few introductory textbooks\textsuperscript{1-3} provide an excellent and thorough bottom-up approach for new researchers entering the field of EPR spectroscopy, but are not designed to provide a short general overview with a wide range of examples. There are however several accessible reviews on specialised topics that the interested reader is referred to: e.g. metallobiomolecules,\textsuperscript{4} \textit{in situ} EPR (heterogeneous catalysis),\textsuperscript{5} and ENDOR.\textsuperscript{6} Here, we aim to close the gap between EPR spectroscopists and chemists not acquainted with EPR, with a tutorial review that provides a basic theoretical background, introduces a representative range of current EPR methods and provides an illustration of the chemical questions that may be answered using this lesser-known and advancing magnetic resonance spectroscopy method.

1.1 EPR versus NMR
NMR spectroscopy (discovered just a year after Zavoisky’s EPR experiments) and EPR share the same fundamental principles and it is useful to begin by comparing these two magnetic resonance spectroscopies (Table 1). Both EPR and NMR probe the interaction of magnetic dipoles with an applied magnetic field and electromagnetic radiation of the appropriate wavelength. Whilst NMR is concerned with the splitting of nuclear spin states in a magnetic field, EPR is concerned with the splitting of electronic spin states. A nuclear magnetic dipole arises from the combined spin of neutrons and protons in a nucleus, whereas an electron magnetic dipole arises from one or more unpaired electrons. However, while most compounds have at least one NMR-active nucleus (\textit{i.e.} I \geq 1/2), usually protons, not all molecules are “EPR active” because most stable molecules have a closed electronic shell. Indeed, EPR
The presence of multiple unpaired electrons ($S > 1/2$) is common in e.g. transition metals and can result in EPR spectra that are much more difficult to interpret (Section 5). A much higher frequency of electromagnetic radiation is required for EPR (microwaves) compared to NMR (radiowaves), and EPR is approximately three orders of magnitude more sensitive than NMR. Consequently, magnetic field strengths are usually much lower in EPR and measurements are typically recorded using electro-rather than superconducting magnets. The most common ‘X-band’ EPR uses a microwave frequency of ~9.5 GHz and an applied field of ~0.3 T. The sensitivity limit in EPR is approximately $10^{13}$ spins, but this value should only be taken as a very approximate reference point because it is hugely dependent on the width of the EPR spectrum (anisotropy, see Section 2.1), the spin system (high spin states with $S > 1/2$ typically require higher spin concentrations) and experimental conditions. The much faster relaxation times (Section 2.8) in EPR have two immediate consequences: unlike NMR, the sample often has to be frozen to enable observation of a spectrum, and lines in EPR spectra are much broader.

1.2 The scope of EPR and of this review

Given the requirement for at least one unpaired electron, one may conclude that few compounds are amenable to EPR spectroscopy. Fortunately, this is not the case since many diamagnetic compounds can be spin labelled, or cycle through functional states that are paramagnetic and that can be obtained through reduction, oxidation, photoexcitation, or trapped using rapid freeze-quench. In this review, we cannot do justice to all the different research areas where EPR spectroscopy is applied, and we do not discuss the instrumental and experimental developments in the field. Rather, we have attempted to choose examples that illustrate the principles we introduce in an accessible manner. Moreover, given the wide scope of EPR spectroscopy, we cannot provide a complete overview of all its applications and we focus on areas that are arguably most relevant to the chemical sciences (green ovals in Fig. 1).

A major and perhaps obvious advantage of EPR spectroscopy stems from the fact that the technique is blind to the many paired electrons in a molecule. Thus, information specifically about the centre with unpaired electron(s) and its interaction with the environment can be obtained. The information that EPR can provide on the structure and dynamics of (bio)chemical systems is heavily reliant on choosing the ‘right’ EPR experiments and on spectral interpretation (Scheme 1). This is turn requires a solid understanding of the magnetic interactions at play. A discussion of the fundamental physical principles behind EPR

---

**Table 1** Comparison between NMR and EPR. Note that for simplicity some generalisations were made: e.g. the resonance frequency

<table>
<thead>
<tr>
<th></th>
<th>NMR</th>
<th>EPR</th>
</tr>
</thead>
<tbody>
<tr>
<td>Spin under investigation</td>
<td>Nuclear spins, often many per molecule</td>
<td>Electron spins, often just one per molecule</td>
</tr>
<tr>
<td>Spin quantum number</td>
<td>$I \geq 1/2$</td>
<td>$S \geq 1/2$</td>
</tr>
<tr>
<td>Magnetic quantum number</td>
<td>$m_s = \pm 1/2$, $\pm 1$, $\pm 3/2$, ...</td>
<td>$m_s = \pm 1/2$, $\pm 1$, $\pm 3/2$, ...</td>
</tr>
<tr>
<td>Characteristic property</td>
<td>Chemical shift</td>
<td>$g$ values</td>
</tr>
<tr>
<td>Resonance frequency</td>
<td>MHz</td>
<td>GHz</td>
</tr>
<tr>
<td>Sensitivity</td>
<td>mM concentrations required</td>
<td>$\mu$M concentrations required</td>
</tr>
<tr>
<td>Relaxation times</td>
<td>$\sim s$</td>
<td>$\sim \mu s$</td>
</tr>
<tr>
<td>Linewidths ($\sim 1/\text{relaxation time}$)</td>
<td>Hz</td>
<td>MHz</td>
</tr>
<tr>
<td>Time resolution</td>
<td>$\sim ms$</td>
<td>$\sim ns$</td>
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</tbody>
</table>

*a Table adapted from third-year physical chemistry lectures notes (2005) by Professor Peter Hore (University of Oxford).*
spectroscopy (Section 2) will provide a framework for the subsequent sections of this review, that present examples falling into the different areas in Fig. 1 (green circles). Indeed, such a foundation is required in order to illustrate what EPR can measure and what information can be gained – and thus what chemical questions may be answered.

2 Fundamental physical principles

The fundamental principles presented in this section are necessarily in abridged form. For accessible introductory textbooks, the reader is referred to the book edited by Brustolon and Giamello (offering a practical approach),4 the recently published EPR Oxford Chemistry Primer (offering an excellent treatment of fluid solutions in particular)1 and the book by Hagen (focussing on biological EPR).2 A more advanced account can be found in Weil and Bolton,11 and the book by Schweiger and Jeschke12 is considered to be the reference work for pulsed EPR principles and spectral interpretation. For experimental aspects of EPR, the reader is referred to Poole.13 In addition, the online book eMagRes14 covers every aspect of modern EPR spectroscopy from instrumentation and methodology to applications in detail.

Here, we have taken a qualitative approach to introduce the fundamental physical principals. The more quantitatively-oriented reader is referred to the text boxes that supplement the text. In order to understand the structure and bonding of a paramagnetic system, we need to understand the different magnetic interactions present as these determine the spacing between energy levels (Box 1). From the transitions between these magnetic energy levels (measured experimentally) energies can be derived and used to deduce information on structure and bonding. In the following sections, we introduce the different types of magnetic interactions. Note that not all of these interactions are necessarily present in any one spin system.

Box 1. Calculating energy levels

The spin Hamiltonian \( H_0 \) enables calculations of the energy levels of the spin system. For a system with a single electron (or multiple strongly-coupled electrons in a single paramagnetic centre) and \( l \) nuclear spins \( H_0 \) is given by:

\[
H_0 = H_{\text{ez}} + H_{\text{nz}} + H_{\text{hf}} + H_{\text{no}} + H_{\text{nn}} + H_{\text{zfs}}
\]

\[ (1a) \]

\[
H_0 = \beta_e B_0 g_S S(S+1)/\hbar + \sum_{i=1}^{l} \alpha_i B_0 I_i(I_i + 1) + \sum_{i=1}^{l} S_i I_i + \sum_{i<j}^{l} \frac{1}{4} I_i I_j + \sum_{i<j}^{l} I_i d_{ij} I_j + \text{SDS}
\]

\[ (1b) \]

where the six energy terms (given in angular frequency units here) describe the electron Zeeman, nuclear Zeeman, hyperfine, nuclear quadrupole, nuclear-nuclear and the zero-field splitting interactions, that are explained in Sections 2.1 to 2.7. In eqn (1b), variables are in italics, vectors and matrices are in bold, \( \beta_e \) is the Bohr magneton and \( \beta_n \) is the nuclear magneton. \( S \) (the electron spin operator with electron-spin quantum number \( S = n/2 \), where \( n \) is the number of unpaired electrons) is analogous to \( I \) (the nuclear spin operator with nuclear-spin quantum \( I \) that depends on the nucleus) in NMR. If more than one non-interacting paramagnetic centre is present, each centre is characterised by its own spin Hamiltonian. For interacting paramagnets (e.g. many dimers or diradicals) additional coupling terms have to be included.
2.1 The electron zeeman interaction ($H_{EZ}$)

This fundamental interaction between the unpaired electron(s) and the applied magnetic field is described by $g$ values that are analogous to the chemical shift in NMR.

The $g$ value can thus be used as an identifier for a given paramagnetic species. Since the unpaired electron is typically bound to a molecule, the $g$ value for a given paramagnet usually deviates from $g_e$ (the free-electron $g$ value, $\sim 2.0023$). The magnitude of the shift depends on the molecular environment and ultimately the spin–orbit interaction (that scales with atomic number); it is small for organic radicals ($g \sim 2$) and can be very large in transition metal or lanthanide complexes. Similar to the chemical shift in NMR, $g$ values are independent of the operating frequency of the instrument. In EPR, the operating frequency, that goes hand in hand with the applied magnetic field strength, refers to the frequency of the microwave radiation of the source. Note that $g$ values designate the intrinsic resonance position of a radical in a particular environment rather than being given relative to a reference compound (like in NMR).

Box 2. $g$ values

$g$ is a $3 \times 3$ matrix (eqn (1b)) that can be diagonalised to yield three principal components $(g_x, g_y, g_z)$ as well as three Euler angles that describe the orientation of this tensor in a given molecular frame. Since $\Delta E = gB_0B_0$ (see Fig. 2) and given that the EPR spectrometer operates at fixed frequency so that $\Delta E$ is a constant, $B_0$ and $g$ are inversely proportional: as the $g$ value decreases the corresponding resonant field increases and vice versa.

The electron Zeeman interaction depends on the applied magnetic field (see eqn (1b) in Box 1). As we shall see in Section 3.1, this field dependence can be exploited when dealing with complex spectra given that, similar to NMR, recording EPR spectra at different magnetic fields allows the separation of field-dependent and field-independent interactions.

2.2 The nuclear Zeeman interaction ($H_{NZ}$)

This interaction between the nuclear spin(s) and the applied magnetic field is analogous to the electron Zeeman interaction but usually only needs to be considered in pulsed EPR.

Given that each nucleus interacts differently with the applied magnetic field, the nuclear Zeeman interaction plays a major role in NMR spectroscopy. The NZ interaction has little effect in CW-EPR spectra (see Box 3), but is significant in pulse EPR.

Box 3. Nuclear $g$ values

Protons have the largest nuclear $g$ value $(g_p)$ of all nuclei, yet their nuclear Zeeman interaction is only 1/658 of the electron Zeeman interaction because of the much smaller mass of the electron ($\frac{e}{2m_p}$ and $\beta_p = \frac{e\hbar}{2m_p}$, where $m_p$ and $e_p$ are the proton mass and charge, respectively). Using $\Delta E_{\text{EPR}} = g\beta pB_0$ and $\Delta E_{\text{NMR}} = g\beta nB_0$, this explains why EPR spectroscopy requires lower magnetic fields and higher frequencies than NMR.

In field-swept EPR spectra (Section 2.9), transitions between nuclear sublevels are forbidden by the selection rules ($\Delta m_p = \pm 1$, $\Delta m_I = 0$), see Fig. 2.

2.3 The electron–nuclear hyperfine interaction ($H_{HH}$)

This interaction between the magnetic dipole of unpaired electrons and surrounding nuclei (typically within 5 Å, e.g. $^1H$, $^{13}C$, $^{14}N$, $^{31}P$, $^{51}V$, $^{63,65}Cu$) is perhaps the most important source of chemical information in EPR.

The hyperfine interaction ($A$) consists of two contributions: the isotropic and anisotropic parts. The isotropic part ($a_{iso}$) is a through-bond interaction and is related to the probability of finding the electron spins at the position of the nucleus, i.e. the occupied orbital must have some s-orbital character (Box 4).

It is noteworthy that isotropic contributions are routinely measured in metals or radicals where the unpaired spin is nominally in p orbitals ($\pi$ radicals, e.g. pentacene radical anion/cation) or d and f orbitals (transition metals and lanthanides). This is because there are mechanisms that transfer (polarise) the spin orientation of the unpaired electron in the p, d, f orbitals to the inner s orbitals. Knowledge of $a_{iso}$ thus allows the mapping of spin delocalisation onto molecular structure, providing information on the nature and spatial extent of the orbital in which the unpaired electron resides.
Box 4. A more quantitative look at the hyperfine interaction

For an electron coupled to a single nuclear spin, the hyperfine Hamiltonian is given by:

\[ H_{\text{HF}} = S A I. \] (2)

The hyperfine matrix \( A \) consists of an isotropic and an anisotropic component:

\[ A = a_{\text{iso}} I + T, \] (3)

where \( I \) is the identity matrix and \( T \) is the dipolar part of the hyperfine matrix. \( a_{\text{iso}} \) (typically in MHz), also known as Fermi’s contact interaction, is proportional to the probability of finding the electron spin at the nucleus \( |c(0)|^2 \):

\[ a_{\text{iso}} = \frac{2 g_e \mu_B \hbar c}{3 h g_e B_0} |\langle 0 | c \rangle|^2 = \frac{\text{Tr}(A)}{3}. \] (4)

It follows from eqn (4) that different isotopes of the same element will display isotropic hyperfine constants proportional to the corresponding \( g_n \) for instance deuterium will have an isotropic hyperfine coupling \( \approx 6.5 \) times smaller than that of hydrogen.

The dipolar part of the hyperfine matrix can be used to determine the distance \( r \) between an unpaired electron \( T \) is proportional to \( 1/r^3 \). In the EPR literature, \( A, a_{\text{iso}} \) and \( T \) are usually given, where

\[ A = [A_x, A_y, A_z] = a_{\text{iso}} + T. \] (5)

\( A_{x,y,z} \) are the principal components of the diagonalized hyperfine matrix and \( T = [-T_z, T_y, T_x] \) in axial symmetry.

The anisotropic part \( T \) is a pure magnetic dipole–dipole interaction that averages out in liquid solution and is thus only detected in the solid state. \( T \) depends on the orientation and the average distance between the unpaired electron and the magnetically active nucleus. Like \( g \) in the solid state, \( T \) has three components \( T_x, T_y, T_z \), along each Cartesian axis. In EPR,
particularly in solids, \( T \) can be used to derive spatial information. Hyperfine EPR spectroscopy has been used to obtain functional information on specific magnetic nuclei, for instance protons that are often ill-defined in structures obtained by other methods,\(^{15}\) or reactive intermediates in microporous materials.\(^{16}\) As shown in Fig. 2B above, the hyperfine interaction results in further splitting of the energy levels and in simple cases \( A \) can be deduced directly from a field-swept EPR spectrum.

2.4 The nuclear quadrupole interaction for nuclei with nuclear spin \( I > 1/2 \) \((H_{\text{NN}})\)

The nuclear quadrupole coupling yields information on the bonding of \( I > 1/2 \) nuclei, e.g. the degree of sp hybridisation, such as distinguishing between an amine and an amide.

This interaction exists only for nuclear spins with \( I > 1/2 \) (e.g. \( ^{2}\text{H}, ~^{14}\text{N} \)), which possess a nuclear quadrupole moment. The nuclear quadrupole interaction stems from the interaction of the nuclear quadrupole moment \((Q)\) with the electrical field gradient generated by the asymmetric distribution of the electron density (Box 5). The nuclear quadrupole interaction can be observed when molecular tumbling is suppressed (since the trace of \( Q \) is zero, Box 5) but due to broadening its effects are often small and difficult to detect in field-swept EPR spectra. Nonetheless EPR spectra with narrow lines can display discernible peak shifts (no additional peak splittings are observed) resulting from the nuclear quadrupole interaction; for an example the reader is referred to Fig. 8 and discussion in ref. 17.

### Box 5. The nuclear quadrupole

The nuclear quadrupole term in the Hamiltonian is given by:

\[
H_{\text{NN}} = iQe\frac{\hbar}{C_0},
\]

where the nuclear quadrupole tensor \( Q \) is traceless (it cannot be observed if the molecule tumbles rapidly). In the eigenframe it is given by

\[
Q = \frac{e^2 qQ}{4(2I-1)\hbar^2} \begin{pmatrix} \frac{1-\eta}{2} & -\frac{1+\eta}{2} \\ -\frac{1+\eta}{2} & \frac{1-\eta}{2} \end{pmatrix}.
\]

The two quantities given in the literature are usually \((e^2 qQ)/\hbar\), the quadrupolar coupling constant, and \( \eta \), the asymmetry parameter (0 < \( \eta < 1 \), where 0 designates axial and 1 rhombic symmetry). Given that a comparison between quadrupolar coupling constants is meaningful only between nuclei with same \( I \), in some cases the quantity \( K = \frac{e^2 qQ}{4(2I-1)\hbar} \) is given in the literature.

The nuclear quadrupole interaction can be apparent in pulse EPR spectra, from which the nuclear quadrupole coupling constant or \( K \) (see Box 5) can often be determined. Indeed \( K \) for \(^{14}\text{N} \) nuclei can be a sensitive probe for the detection of hydrogen bonding.\(^{15,18} \)

2.5 The nuclear–nuclear spin interaction \((H_{\text{NN}})\)

Although essential in NMR, nuclear–nuclear spin interactions are negligible in EPR given their small relative magnitude compared to electron–nuclear and electron–electron interactions.

2.6 Strongly-coupled electrons: the zero-field splitting interaction \((H_{\text{ZFS}})\)

The zero-field interaction can become very important when multiple strongly-coupled unpaired electrons are present (e.g. electrons located on the same transition metal ion).

When more than one electron spin is present the electron–electron coupling also has to be considered. Strongly-coupled unpaired electrons are well-described by a ‘group spin’, \( S > 1/2 \). The dipolar and spin–orbit coupling between such strongly interacting electrons removes the \((2S + 1)\) degeneracy expected in the ground state – this zero-field splitting is, as the name suggests, present even in the absence of a magnetic field (Box 6). The two zero-field splitting parameters, \( D \) and \( E \), depend on the average distance between the unpaired electrons and the deviation from the cubic symmetry, respectively. When the energy of the microwave quantum exceeds the energy gap caused by the ZFS interaction (i.e. \( \hbar \gg D \)), both intra- and inter-manifold transitions are observed (see Box 6 and ref. 19). If on the other hand \( D \gg \hbar \), no inter-manifold and only the intra-manifold transition is observed. The intra-manifold transition can be treated as an effective \( S = 1/2 \) spin system but with \( g \) values that may deviate substantially from those of a ‘true’ \( S = 1/2 \) system.

In this limit, interpretation tools called rhombograms\(^{2} \) have been developed to correlate the effective \( g \) values to the ZFS parameters \((E/D\) ratio\). If the assumption \( D \gg \hbar \) does not hold true, the measured \( g \) values do not follow the rhombogram predictions and may vary when measured at different magnetic fields.

2.7 Weakly coupled electrons: the dipolar and exchange interactions \((H_{\text{dd}} + H_{\text{ex}})\)

The dipolar interaction provides information on the distance and orientation between two weakly-coupled unpaired electrons. The exchange interaction can provide information on the type of coupling, e.g. antiferromagnetic or ferromagnetic.

When two (or more) weakly-coupled electrons are present (e.g. a bis-radical or a di-nuclear \( \text{Cu}^{2+} \) complex with a distance between the spins of ca. 15 Å or more), these are best described by their individual spins, but with consideration of the interactions between them. The electron dipole–dipole interaction is a through-space interaction that, like the electron–nuclear anisotropic hyperfine interaction, depends on the distance \( r \)
Box 6. The zero-field interaction
The zero-field interaction tensor $D$ is symmetric and traceless:

$$D = \begin{pmatrix} D_x & D_y & D_z \\ D_y & D_z & D_x \\ D_z & D_x & D_y \end{pmatrix} = \begin{pmatrix} -\frac{D}{3} + E \\ -\frac{D}{3} - E \\ \frac{2D}{3} \end{pmatrix}.$$  

(8)

therefore only two parameters ($D = 3D_x/2$ and $E = (D_y - D_z)/2$) are needed to describe $D$ in its diagonal form. For cubic symmetry $D = 0$ and the spin sublevels are degenerate; for axial symmetry $D \neq 0$ and $E = 0$, and for rhombic symmetry $D \neq 0$ and $E \neq 0$.

For the $S = 5/2$ example shown here with axial symmetry ($D > 0$, e.g. high-spin Fe$^{3+}$), the $m_s$ sublevels $\pm1/2, \pm3/2$ and $\pm5/2$ are non-degenerate and EPR transitions may be observable at zero field (brown double-headed arrows).

In the presence of $B_{\text{iso}}$, the sublevels are split by the EZ interaction and the black vertical double-headed arrow indicates the intra-manifold EPR transition ($m_s = -1/2 \rightarrow m_s = +1/2$, which for a semi-integer spin is always detectable at any microwave frequency) whereas the blue ones indicate inter-manifold transitions.

between two spins ($1/r^3$) and their relative orientation (Box 7). If there is overlap between the wavefunctions of the two electron spins, an additional contribution, stemming from the electron exchange interaction (Box 7), must be considered. In the simple case of two $S = 1/2$ spins, the sign of the isotropic exchange interaction $J_{\text{iso}}$ determines whether the singlet state (antiferromagnetic coupling, positive $J_{\text{iso}}$) or the triplet state (ferromagnetic coupling, negative $J_{\text{iso}}$) lies lower in energy. Because the electron exchange interaction decays exponentially with distance as the wavefunctions of the overlapping orbitals decay, $J_{\text{iso}}$ normally tends to zero at distances greater than approximately 15 Å.

Box 7. A closer look at weakly coupled spins
For two weakly-coupled electron spins (1 and 2) the spin Hamiltonian is given by:

$$H_0 = H_d(S_1) + H_d(S_2) + H_{\text{iso}} + H_{\text{ex}}$$  

(9a)

$$= H_d(S_1) + H_d(S_2) + S_1D_{S_2} + S_1JS_2.$$  

(9b)

where $H_d(S_1)$ and $H_d(S_2)$ are defined by the energy terms given in Box 1. The electron dipole–dipole coupling tensor $D$ (note that, confusingly, $D$ is also used for the zero-field splitting tensor) is analogous to $T$ (see Box 4):

$$D = \frac{\mu_0}{4\pi} \frac{\mathbf{r}_1 \cdot \mathbf{r}_2}{r^3} \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & -1 \end{pmatrix} = \begin{pmatrix} -\alpha_{dd} & 0 & 0 \\ 0 & -\alpha_{dd} & 0 \\ 0 & 0 & 2\alpha_{dd} \end{pmatrix}.$$  

(10)

This point-dipole approximation of $D$ is not always valid, especially when the $g$-anisotropy is large (e.g. transition metal ions) and the electron spin is highly delocalised (e.g. iron–sulfur clusters).

The electron exchange coupling tensor $J = \begin{pmatrix} -J & -J & -J \\ -J & J & -J \\ -J & -J & J \end{pmatrix}$ consists of an isotropic ($J_{\text{iso}}$) and an isotropic part. $J_{\text{iso}}$ is usually sufficient to describe the exchange coupling:

$$H_{\text{ex}} = J_{\text{iso}}S_1S_2.$$  

(11)

Several conventions are used in the literature, $(-J_{\text{iso}}S_1S_2, 2J_{\text{iso}}S_1S_2, -2J_{\text{iso}}S_1S_2, J_{\text{iso}}(2S_1S_2 - 1/2))$, so that it is important to check which expression was used in order to determine $J_{\text{iso}}$.

2.8 Relaxation ($T_1$ and $T_2$)
Fast relaxation times mean that many samples have to be measured in the frozen state. Provided that relaxation times are sufficiently fast, the sensitivity of an EPR experiment generally increases with decreasing temperature, as expected from the Boltzmann distribution.
In addition to the “static” interactions discussed in the previous sections, two dynamic relaxation processes play an important role in an EPR experiment: (1) the spin–lattice or longitudinal relaxation time \( T_1 \) characterises spins ‘dropping’ from the upper energy level to the lower level with excess energy dissipated through thermal vibrations of the lattice; (2) the spin–spin or transverse relaxation time \( T_2 \) characterizes the redistribution of energy within an ensemble of spins and occurs with no net energy change. In the absence of relaxation, the application of microwave radiation would equalise the populations of the lower and upper energy levels so that no net microwave radiation would be absorbed and no EPR signal observed. Relaxation, which re-establishes equilibrium populations, is thus required to remove this microwave “saturation” effect and allow observation of an EPR signal. On the other hand very fast relaxation, as often observed at room temperature for e.g. transition metal complexes, can lead to such extensive broadening of the spectrum (see eqn (12) in Box 8) that effectively no EPR signal is observed. Because \( T_1 \) and \( T_2 \) increase with decreasing temperature, such ‘fast-relaxing’ systems can often be investigated at cryogenic temperatures. Analysis of relaxation times and their dependence on molecular orientation in the applied magnetic field\(^{20}\) can provide valuable insight into molecular and lattice dynamics, e.g. organic radicals and transition metals.\(^{21}\)

Box 8. A closer look at relaxation

\[ T_1 \text{ and } T_2 \text{ are related to the (homogeneous) linewidth through the following equation:} \]

\[ \frac{1}{\Delta \omega} = \frac{1}{2 \pi T_1} + \frac{1}{2 \pi T_2} \]

\( T_1 \) affects linewidths because it is related to the lifetime of the upper energy level: a long \( T_1 \) leads to sharper lines, and vice versa, as dictated by Heisenberg’s uncertainty principle. \( T_2 \) affects the linewidth through spin–spin dipolar and exchange interactions.

Given that \( T_1 \) (typically ns) \( > T_2 \) (typically \( \mu \)s), \( T_2 \) tends to dominate the line broadening. \( T_m \) (the phase memory time) is a useful parameter to characterise the resultant linewidth, as well as the echo decay in many pulse EPR experiments.

2.9 Experimental considerations

Continuous wave (CW) measurements are usually the entry point for any EPR investigation. Pulse EPR measurements are needed to investigate a specific (e.g. hyperfine) interaction in detail and almost always require cryogenic temperatures (i.e. solid-state samples).

A basic knowledge of how EPR spectrometers operate\(^{22}\) is required in order to acquire reliable data. Commercially available EPR spectrometers span a microwave frequency of 1 to 263 GHz (corresponding to a magnetic field of 0.03 to 9 T), but most EPR studies are conducted at 9 GHz (~0.3 T), the so-called ‘X-band’ frequency. Q-Band frequency (~35 GHz) experiments are also relatively common. The naming of the different frequency bands in EPR has a historical origin dating back to the development of radars. EPR experiments conducted at higher microwave radiation (and hence magnetic field strength) can be more sensitive but are also usually more involved experimentally. Since fluid-solution EPR spectra are very sensitive to molecular motion and their shape reflects the complete or incomplete averaging of any magnetic interaction (e.g. g values, hyperfine interactions, dipolar interactions), it follows that the operating frequency (i.e. the applied microwave frequency, \( \nu_{\text{mw}} \)) can greatly affect the appearance of the spectrum. For example, a radical with anisotropic axial g values of \( g_x = 2.15 \) and \( g_z = 2.00 \) will give rise to an EPR spectrum with a single line at \( \nu_{\text{mw}} = 2.10 \) provided that the radical tumbling time is less than the \( 1/\nu_{\text{mw}} \) (e.g. 100 ps at 9.5 GHz or 10 ps at 95 GHz). Conversely, if the radical tumbling time is greater than \( 1/\nu_{\text{mw}} \), the EPR spectrum will show two lines, a superposition of \( g_x \) and \( g_{xy} \). The above generalisation only holds true when the magnetic anisotropy is relatively small; a larger anisotropy requires lower operating frequency or faster tumbling to be averaged out. Indeed, an intermediate regime between these two extremes is most commonly observed. In summary, dynamics that are fast at X-band, and lead to a complete averaging of the magnetic anisotropies, may appear slow at W-band. Sample conditions such as solvent viscosity and temperature can also have a profound effect on EPR spectra given their influence on molecular dynamics.

2.9.1 CW EPR. In a CW experiment the sample is irradiated continuously by low-intensity monochromatic microwave radiation. As the magnetic field is swept over a defined range, different EPR transitions are brought into resonance by the applied microwave radiation. CW field-swept spectra are typically measured and presented as derivatives because a modulation-amplitude detection method is used experimentally. This method of detection leads to an increased signal-to-noise ratio. Although convenient and often the first step required for a more in-depth study, CW EPR usually suffers from limited spectral and time resolution. Similar to NMR, CW EPR spectra simplify considerably when recorded in fluid solution, i.e. when molecules are free to tumble and magnetic interactions are averaged such that only isotropic components survive: in fluid solution all molecules are equivalent and experience the same average interaction with the applied magnetic field (see Fig. 2A and ref. 1 for a detailed description). In frozen solution the orientation of each molecule is fixed with respect to the applied field and consequently the magnitude of the interactions is different. The CW spectrum of a frozen solution is a weighted sum of all the possible molecular orientations. Therefore, all but the largest electron–nuclear spin interactions (hyperfine couplings) are masked by the relatively broad linewidths.

2.9.2 Pulse EPR. Akin to modern NMR, in a pulsed EPR experiment the field is kept constant and the sample is irradiated with short (nanosecond) and high-intensity microwave pulses. A pulsed experiment enables isolation, detection and measurement of the interactions that contribute to the shape and behaviour of a CW spectrum (Box 9). Importantly, pulse
EPR experiments can be designed to address a specific interaction (i.e. a specific term in the spin Hamiltonian, Box 1). Because relaxation times are too short at room temperature, pulsed EPR measurements normally require cryogenic temperatures. In the examples discussed in Sections 4 and 5 we thus restrict our discussion to powder and frozen-solution samples. The requirement for solid-state samples for pulse EPR has the advantage that we can measure dipolar magnetic interactions that are suppressed by motional averaging in liquid solution.

### Box 9. Anisotropy in pulse EPR

The large anisotropy of some powder/frozen samples (i.e. their EPR spectra span a large magnetic field range) can be used to derive orientation-specific information, for example the measurement of $A_e$ specifically. That is, measurements at specific field positions can yield “single crystal-like” information, i.e. as if measuring a single crystal in a specific orientation with respect to the applied magnetic field. However, in many cases the full set of magnetic parameters ($A_e, A_y, A_z$) cannot be determined ‘by eye’ from a single spectrum. Simulation of spectra acquired at a set of different field positions is required because of ‘orientation selection’, i.e. the applied microwave pulse cannot excite the entire EPR spectrum (for example, an Fe–S cluster spectrum typically spans 40 mT when the microwave pulse excitation bandwidth is only a few mT). However, the recent introduction of shaped and composite pulses, which open the possibility of independently tuning the amplitude and phase of microwave pulses, already improves excitation bandwidths, can remove orientation selection, and promises to revolutionise EPR spectroscopy.

### 2.9.3 Pulse EPR experiments

Here, we briefly introduce some of the most common pulse EPR experiments that are referred to in the following sections. For full descriptions, including pulses sequences, see ref. 12.

#### Echo-detected field sweeps (Box 10)

Echo-detected EPR experiments are mostly based on the detection of the free induction decay (FID) of magnetization after a radiowave pulse (A):

**Box 10. Echo-detected EPR**

NMR experiments are mostly based on the detection of the free induction decay (FID) of magnetization after a radiowave pulse (A):

**ENDOR.** In electron–nuclear double resonance (ENDOR) experiments, NMR transitions (i.e. transitions involving nuclear spin flips, which are nominally EPR-forbidden) are driven by a radiofrequency radiation. ENDOR often provides very useful information on strongly coupled nuclei, e.g. those in the first coordination sphere of the electron spin. For a tutorial review on ENDOR spectroscopy, including continuous-wave ENDOR and the most common Mims and Davies pulse sequences, the reader is referred to ref. 6.

**ESEEM.** The information derived from electron spin echo envelope modulation (ESEEM) experiments is analogous to that obtained from ENDOR, i.e. both experiments may be regarded as an NMR spectrum of the paramagnetic compound, with the exception that ESEEM typically detects more weakly coupled nuclei (e.g. those in the second coordination sphere of the electron spin). ESEEM consist of a series of microwave pulses at a single microwave frequency separated by fixed and variable time intervals. The resulting electron spin echo is then recorded as a function of the variable time interval. The pulse sequence induces modulation of the amplitude of the detected electron spin echo that results from magnetic nuclei in the spin system, and yields a modulated time domain signal (similar to a free induction decay). Fourier transformation then allows identification of nuclear frequencies and corresponding hyperfine couplings. For a discussion of different ESEEM experiments (2-pulse and 3-pulse ESEEM), including their advantages and disadvantages, the reader is referred to ref. 23.

**HYSCORE.** When more than one hyperfine coupling is expected to be present, the two-dimensional counterpart of ESEEM – HYSCORE (Hyperfine sublevel correlation) spectroscopy – is often the method of choice. HYSCORE spectroscopy correlates nuclear transition frequencies ($\nu_a, \nu_b$) in the $\alpha$ and $\beta$ electron-spin manifolds (see Fig. 2Bi). The spectrum is divided into two quadrants: signals in the right-hand-side ($+$+$\uparrow$) quadrant typically originate from weakly coupled nuclei ($|A| < 2|\nu_1|$, where $\nu_1$ is the Larmor frequency of the nucleus), whereas those in the left-hand-side ($-$+$\uparrow$) quadrant usually result from strongly coupled nuclei ($|A| > 2|\nu_1|$). The nature of the coupled nucleus can be identified by the position of the peaks in the spectrum, e.g. weakly-coupled $^1$H are centred around the Larmor frequency of the proton (ca. 15 MHz at X-band). The spatial separation of different types of nuclei, and whether they are weakly-coupled...
or strongly-coupled explains the popularity of HYSCORE. This technique is however much more time-consuming than one-dimensional ESEEM.

DEER. The double electron–electron resonance (DEER) experiment is often the method of choice to measure the distance between two weakly-coupled electron spins. It is a two-frequency (pump and probe) experiment that measures the electron dipole–dipole interaction between two spins, which varies inversely with their cubed distance. The first microwave frequency is used to select a fraction of the spins (probe) and to produce the measured signal (echo). A second microwave frequency (pump) is used to invert the orientation of the coupled spin, causing a modulation of the signal (echo) intensity at the frequency of the electron spin–spin coupling (known as the dipolar frequency).

2.10 Spectral interpretation

Simulation is usually required for the interpretation of EPR spectra but is increasingly accessible to non-specialists.

Box 11. Why is the interpretation of EPR spectra not straightforward?
EPR spectra often depend on the magnitude and relative orientation of all magnetic tensors (g, A, Q, D) with respect to each other and with respect to the applied magnetic field. This leads to many parameters, but simulations often allow the determination of these tensors and their relative orientation.

In some cases (e.g. when many interactions are of similar magnitude), fitting of the experimental data based on a full quantum mechanical computation (density functional theory) and molecular dynamics simulations is necessary for reliable spectral interpretation.

3 What g values can tell us and the benefit of multiple frequencies ($H_{EZ}$)

In this section we discuss how the interaction between a paramagnet and the applied magnetic field leads to the appearance of an EPR line at a characteristic g value that depends on the molecular environment and the electronic ground state. Owing to their dependence on spin–orbit coupling, g values are much more difficult to predict than NMR chemical shift values and tables correlating g with structural motifs are limited.$^{27,28}$ Nonetheless, g values can be important parameters in EPR characterisation. The relevance of g as an observable to characterise the electronic state and molecular geometry, and the detection of mechanistically-relevant bonding interactions is illustrated below. The advantages of multi-frequency EPR to disentangle composite spectra will also be apparent.

3.1 Detecting the presence of different species and deducing electronic configurations

Motivated by the role that Ti(III) compounds play in homogeneous and heterogeneous catalysis (e.g. Ziegler–Natta polymerisation), Chiesa, Van Doorslaer and co-workers investigated TiCl$_3$(Py)$_3$ and TiCl$_5$ complexes.$^{29}$ Continuous-wave EPR spectra at multiple microwave frequencies (Fig. 3) revealed the presence of two distinct rhombic Ti(III) ($[\text{Ar}]3d^1$, hence $S = 1/2$) species. The g values of the peak positions remain unchanged with increasing magnetic field, indicating that any magnetic interaction between the centres is negligible (see, in contrast, Section 3.2). The two Ti$^{3+}$ species could in fact be ascribed to defects in the solid, ligated by $^{14}$N nuclei (as revealed by pulse EPR experiments, not discussed here). In this case, the only magnetic interaction that needs to be considered is the EZ interaction for the two Ti(III) species since other interactions are not resolved (i.e. the spin Hamiltonian is well described by $H_{EZ}$, see eqn (1), Box 1).

Few spectra can be fully and easily interpreted by measuring peak positions and separations like in one-dimensional NMR (Box 11). Spectral interpretation is often the most time-consuming aspect of any EPR study and usually requires simulation of the EPR spectra. Historically, simulations were a major bottleneck, with each research group having to develop their own programmes. Nowadays a number of excellent packages are available. One of the best is EasySpin, a toolbox supported by MATLAB for simulating and fitting CW and pulsed EPR spectra (http://easyspin.org).$^{24,25}$ The now widespread use of EasySpin, which is freely available, enables consistent analysis and allows non-experts to simulate most EPR spectra. EPR spectrometers manufacturers have also developed simulation packages (e.g. XSophe by Bruker). In addition, the fast open-source spin dynamics programme Spinach covers magnetic resonance applications, including EPR (http://spindynamics.org/Spinach.php).$^{26}$ Finally, the on-line educational tool EPR simulator (http://www.eprsimulator.org),† enables the user to see the effect of different EPR parameters on simulated spectra (e.g. Cu(II), nitroxides, radicals in solution) in an interactive manner.

Fig. 3. Two distinct Ti(III) species present in powder TiCl$_3$(Py)$_3$, as revealed by multifrequency EPR. Simulated EPR spectra are in red. Adapted from ref. 29 with permission from the PCCP Owner Societies.

† EPR Simulator is under construction and being developed by Dr Victor Chechik, University of York (UK).
Jahn–Teller distorted Cu$^{2+}$. The vast majority of Cu$^{2+}$ complexes state and the geometry of metal complexes. A classic example is $B_{g}$ in the 3d$^{9}$ of tetragonal distortion), and thus in the unpaired electron being can result in 'shortening' of the $z$ axis (a much less common type of tetragonal distortion), and thus in the unpaired electron being in the 3d$\alpha$ orbital, $g_{z} > g_{\alpha,\beta}$ (see Fig. 4, left). This is clearly apparent in the Q-band ($\sim 35$ GHz) CW EPR spectra (Fig. 4, right). Note that the hyperfine coupling of the electron spin to the Cu nuclear spin $(I = 3/2, 2I + 1 = 4)$ is, as is often the case, only resolved along $g_{z}$.

3.2 Inferring magnetic coupling between centres through $g$ values

EPR spectroscopy led to the discovery of iron–sulfur (Fe–S) clusters, which are now recognised to be ubiquitous in nature and assume a wide range of roles ranging from electron transfer to participation in catalysis. It was long a puzzle how two Fe ions (high-spin Fe$^{3+}$, $S = 5/2$, and Fe$^{2+}$, $S = 2$, both have expected $g$ values above $g_{e}$) give rise to an average $g$ value below $g_{e}$. Long before the first crystallographic structures became available, Gibson et al. predicted an antiferromagnetic exchange interaction between the Fe centres, forming a [2Fe–2S] cluster, that explains the experimentally observed $g$ values and the total spin $S_{\text{total}} = S_{\text{Fe(III)}} - S_{\text{Fe(II)}} = 1/2$ ground state (Fig. 5).

3.3 Detecting mechanistically relevant bonding interactions

Radicals are involved in numerous redox reactions and biological electron transfer, and deciphering their bonding interactions is of mechanistic relevance. Stoll et al. showed that hydrogen bonding to tryptophan radical cations is reflected in a change in the $g$ anisotropy. The very small shift of $g_{\alpha}$ by just 0.00015 (Fig. 6), that could be predicted by density functional theory, is only detectable at extremely high magnetic fields/frequencies (700 GHz). Pulse ENDOR (Section 2.9) at lower frequencies (X- and Q-band) however could detect the H-bonded proton by comparison with the deuterated sample. The very different magnetic properties of $^{1}\text{H}$ ($I = 1/2$) and $^{2}\text{H}$ ($I = 1$) mean that deuteration is commonly employed to detect and characterise exchangeable protons, and the effects of isotopic substitution on EPR spectra are discussed further in Section 4.4.
All discussion in this section was restricted to $S = 1/2$ systems. Large deviations from $g_e$ can occur in systems with multiple unpaired electrons (see Section 5).

### 4 Nuclei surrounding the unpaired electron spin: Hyperfine and nuclear quadrupole interactions ($H_{HF}$ & $H_{NQ}$)

In this section we will show that a wealth of information can be extracted from the interaction between unpaired electrons and surrounding nuclei, that not only encodes structural but also functional and mechanistic information. In the examples below, the reader will be introduced to some of the most common experiments used to measure and gain more detailed information from hyperfine interactions. More than a single EPR method is often suitable (and necessary) to solve a particular problem, and the examples below have been chosen to illustrate different hyperfine EPR experiments (see Section 2.9.3).

#### 4.1 Fe(i) intermediate in catalysis (CW EPR)

Organometallic Fe(i) compounds are rare but were recently shown to be important intermediates in Negishi cross-coupling reactions through EPR experiments. Continuous-wave EPR spectroscopy of a likely Fe(i) intermediate shows that the unpaired electron is primarily located on the low-spin Fe centre ($S = 1/2$), with a near-axial $g$ tensor (Fig. 7) whose anisotropy was reproduced in DFT calculations. Moreover, large hyperfine couplings to four nearby phosphorus atoms ($I = 1/2$) are clearly visible. From the $1:4:6:4:1$ quintuplet pattern apparent in the $g_1$ region and on the basis of the structure one may be led to conclude that the strength of the hyperfine coupling to the Fe(i) electron spin of the two (equal) equatorial P is very similar to the two (equal) axial P. However, as revealed through simulation of the entire EPR spectrum, the equatorial $^{31}$P are actually inequivalent and one is more weakly coupled ($a_{iso} = 37.9$ MHz, $T = [2.9, -5.7, 2.7]$ MHz, see Box 4) relative to the remaining P ligands with similar coupling parameters ($a_{iso} = 71$ MHz, $T = [2.8, -1.4, -1.4]$ MHz). EPR experiments thus demonstrated unambiguously that Fe(i) is present in such cross-coupling reactions, and that the complex adopts a distorted geometry in solution as shown by the inequivalent spin density distribution onto the $^{31}$P ligands.

#### 4.2 Host–guest interactions (ENDOR)

Unless the hyperfine coupling to the electron spin is relatively large (tens of MHz), it is often not observed in CW EPR in the solid state. We now discuss an example of a much subtler interaction. Turro and co-workers investigated the magnetic communication between a fulleride radical anion host cage and a H$_2$ guest molecule encapsulated within it (Fig. 8). The H$_2$ guest can be in the ortho ($I = 1$) or para ($I = 0$) nuclear spin state. The CW EPR spectrum (Fig. 8A) is dominated by three lines of approximately equal intensity, arising from the unpaired electron delocalised over the surface of the fulleride. However, pulsed ENDOR spectroscopy revealed the weak coupling between the unpaired electron and the endo-H$_2$ molecule through difference spectra (Fig. 8B). In this ‘weak-coupling case’ ($\nu_i > A/2$), the observed peaks are centred around the Larmor frequency of the proton ($\nu_l \approx 14.8$ MHz) at the measurement field as shown in Fig. 8B ($A = [0.35, 0.35, -1.00]$, i.e. $A_{iso} = -0.10$ MHz and $T = -0.45$ MHz, see Box 4). On the basis of the magnetic interaction between the fulleride and the H$_2$ molecule, demonstrating that cage and host molecule ‘communicate’, and the observed temperature dependence of the ENDOR spectra (not discussed here) showing that the ortho–para interconversion takes no longer than 1 hour, the authors conclude that spin catalysis is highly efficient and may lead to a new way of driving ortho-H$_2$/para-H$_2$ conversion.

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Note the notation $g_{1,2,3}$ (rather than $g_{x,y,z}$) is used in this case because the $g$ values were not assigned to the Cartesian axes.

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Fig. 6 Illustration of how $g$ values can be sensitive to relatively weak bonding interactions. The $g_x$ of the tryptophan radical cation shifts with hydrogen bonding, as revealed by very high-frequency EPR (700 GHz). In deuterated samples the proton of HX (in red) is replaced by D. Adapted with permission from ref. 34. Copyright 2011 American Chemical Society.

Fig. 7 Fe(i) complex in Negishi cross-coupling reactions (left, schematic structure) and corresponding X-band CW EPR spectrum and simulation (right) demonstrating that the unpaired electron is mostly located on Fe. Note that the indicated hyperfine couplings $A$ are very approximate but serve as a good starting point for simulations (a useful rule of thumb is that 1 mT ~ 28 MHz for $g \sim 2$). Adapted with permission from ref. 35. Copyright 2012 American Chemical Society.
4.3 The interstitial atom in the nitrogenase MoFe cluster (ESEEM)

The co-called MoFe cluster is one of the most complex clusters found in nature and being paramount for ‘fixing’ N2 (breaking the nitrogen triple bond to form ammonia), by a mechanism that is not fully understood, continues to be an inspiration for biochemists and chemists alike. The nature of the central interstitial atom (formally coordinated by six bonds) was long a debate that EPR spectroscopy has helped to resolve in conjunction with high-resolution X-ray crystallography. Upon labelling with 13C isotopic labelling. This can allow detection of usually silent nuclei, providing means to characterise intermediates structurally and validate or rule out possible catalytic reaction pathways.

Selective 13C labelling of MDTB revealed signals (correlation ridges), centred around the Larmor frequency of 13C (3.8 MHz at 355 mT), that were not visible in the natural-abundance sample (Fig. 10A); the relatively large aiso (2.7 MHz, see Box 4) shows that significant electron density is on the 13C atom, suggesting that it is directly bonded to the Fe–S cluster, as corroborated by the relatively large axial anisotropy (T = 1.5 MHz, Box 4). The simulated spectrum of the 13C coupling (in the absence of orientation selection, see Box 9) is shown in Fig. 10Bii (right) – note that the experimental spectrum (Fig. 10Bii, left) shows only part of the full ridge required to determine the hyperfine parameters (and hence aiso and T) directly from the spectrum.

Indicative of the two inequivalent N in the side-chain Arginine, the HYSCORE spectrum of the 15N-Arg substituted enzyme (Fig. 10Bii) shows the presence of two sets of peaks, centred around –A/2 in the left-hand quadrant (resulting from the strongly-coupled blue N in Fig. 10C) and the Larmor frequency of 15N in right-hand quadrant (resulting from the weakly-coupled green N in Fig. 10C), respectively. The corresponding 14N spectrum is considerably more complicated; up to 18 cross-peaks may be observed owing to the quadrupole moment arising from the I = 1 nucleus. Usually the most prominent (often sole) peaks are those arising from the so-called double-quantum (dq) transitions (ΔmI = ± 2 in each mI manifold, Fig. 10D) and the hyperfine coupling A can be estimated from these (Fig. 10Bi). Determining the nuclear quadrupole parameters can be useful to deduce structural information such as the degree of sp hybridisation and hence coordination of the N nucleus in question. Although this is often a challenging task, for the strongly-coupled 15N in this example they are readily obtained because the nuclear Zeeman and hyperfine interactions are of similar magnitude and approximately cancel each other out (i.e. combined they have no net effect on the energy levels) in one of the mI manifolds. 

Fig. 9 The MoFe cluster found in nitrogenases showing the usual central C atom with nominally six bonds (left; colour coding: Fe = grey, S = yellow, Mo = brown, central C = highlighted red, protein backbone = black, O = red, N = dark blue) and 3-pulse ESEEM spectra in the frequency domain of the wild-type (wt), 15N- and 13C-labelled protein. The inset show experiments acquired at different r values (see Box 10); this is a requirement for 3-pulse ESEEM experiments because these are affected by blind spots (a suppression effect where individual peaks in the spectrum can disappear completely). Adapted from ref. 37. Reprinted with permission from AAAS.

4.4 Distinguishing between possible reaction intermediates (HYSCORE)

HYSCORE spectroscopy can be used to elucidate catalytic mechanisms and a powerful strategy is to combine HYSCORE with isotopic labelling. This can allow detection of usually silent nuclei (e.g. 12C to 13C, I = 1/2, substitution) or spectral simplification (e.g. 14N, I = 1, to 15N, I = 1/2, substitution). As seen is Section 2.8.3, HYSCORE can distinguish between strongly and weakly coupled nuclei, providing means to characterise intermediates structurally and validate or rule out possible catalytic reaction pathways.

Fugate et al.38 used HYSCORE to distinguish between three intermediates proposed to lead to the formation of biotin, an essential vitamin. The structure of the intermediate deduced from the spectroscopic data is composed of a reduced [2Fe–2S] cluster with a total spin S = 1/2 ground state (see Section 3.2) bonded to 9-mercaptopodethiobiocin (MDTB) as shown in Fig. 10C. The simulated spectrum of the 13C coupling (in the absence of orientation selection, see Box 9) is shown in Fig. 10Bii (right) – note that the experimental spectrum (Fig. 10Bii, left) shows only part of the full ridge required to determine the hyperfine parameters (and hence aiso and T) directly from the spectrum.
the Larmor frequency of $^{14}\text{N}$ at field of the measurement, 347.5 mT, is 1.1 MHz and $\alpha_{\text{iso}} = 3.5$ MHz), as illustrated in Fig. 10D. The nuclear quadrupole transitions $n_0$, $n_0/C_0$ and $n_0 + (n_0 = 2KZ)$, $n_0 + = K(3 + Z)$, $n_0/C_0 = K(3 + Z)$, where $n_0 + n_0/C_0 = n_0 +$ and $K = e^2Q/4h$ (in MHz) for $I = 1$, see also Box 5) are then directly observable (Fig. 10Bi) and nuclear quadrupole parameters $e^2Q/4h$ and $Z$ can be determined easily.40 This “cancellation” or “matching” condition is surprisingly common for $^{14}\text{N}$ because it occurs even when $2|n_I|$ does not appear to match $|\alpha_{\text{iso}}|$ very well. In fact, $n_0$, $n_0/C_0$ and $n_0 +$ are observed as long as $|n_0| = |n_0/C_0|/2K \sim 0.75–1$ (in the example given this ratio approaches the upper limit of 1). In many cases, the condition can be deliberately achieved by changing the microwave frequency.41

5.1 Metal centres

Owing to their partially occupied d orbitals, transition metals often possess unpaired electrons and are thus amenable to EPR studies. In the EPR literature, low-spin refers to $S = 1/2$ systems whereas high-spin pertains any $S > 1/2$ system; the terminology thus differs from that of coordination chemistry (e.g. a “low-spin” $d^4$ octahedral complex is termed a high-spin $S = 1$ system in EPR). When there is a considerable exchange interaction between two or more spins (e.g. two metal centres sharing a μ-oxo bridge or two radicals covalently linked together) it is often convenient to define a total spin $S_{\text{total}}$. If spins are ferromagnetically coupled, $S_{\text{total}}$ is the sum of the individual spins. For anti-ferromagnetically coupled spins, $S_{\text{total}}$ is the difference of the individual spins (see Sections 3.2 and 5.1.2 for examples).

Integer spins ($S = 1, 2, \ldots$) are often difficult to observe in standard (parallel-mode) EPR because the zero-field splitting (ZFS, Section 2.6, Box 6) usually exceeds the energy of the microwave photons and their study typically requires high microwave frequencies beyond the conventional X- to W-bands. The ZFS varies greatly amongst different metal ions and coordination geometries as it depends on the spin–orbit coupling (see Section 3.1 for the effect of spin–orbit coupling on $g$), for instance it is very small for symmetric Mn(ii) complexes and very large for octahedral Co(ii) complexes. A comprehensive review on (high-field) EPR of mononuclear transition metal complexes can be found in ref. 42.
5.1.1 Interaction between multiple spins (exchange coupling).

With the goal to employ molecular nanomagnets as possible qubits (a qubit is a quantum bit of information) Winpenny, McInnes and co-workers used supramolecular chemistry to link two \{Cr\textsubscript{7}Ni\} heterometallic rings \( (S_{\text{total}} = \frac{1}{2}) \) due to antiferromagnetic coupling between 7 Cr(III) ions \( (S = \frac{3}{2}) \), and 1 Ni(II) \( (S = 1) \), Fig. 11B) to a Co(II) complex \( (S = \frac{3}{2}) \). In this three-spin system, the central Co atom is exchange coupled to the neighbouring \{Cr\textsubscript{7}Ni\} heterometallic rings (Fig. 11A). EPR was used to determine the weak interactions between molecular components in the supramolecular structure that are undetectable using magnetometry. The ZFS of the central cobalt is too large to allow detection of intermanifold EPR transitions (see Box 6, even at 94 GHz). The Co\textsuperscript{2+} complex can be treated as an ‘effective’ \( S = 1/2 \) system with ‘characteristic’ \( g \) values that differ greatly from \( g_{z} \): \( g_{z} = 6.5 \) (occurring at \( B \approx 1000 \text{ mT} \) in Fig. 11C), \( g_{y} = 4.3 \) (\( B \approx 1600 \text{ mT} \)) and \( g_{x} \approx 2 \) (\( B \approx 3500 \text{ mT} \)). The two heterometallic rings give rise to EPR signals at \( g_{x,y} \approx 1.78 \) and \( g_{y} \approx 1.74 \), that partially overlap with the \( g_{x} \) signal of the Co(II) centre (Fig. 11C). The four additional splittings (a doublet of doublets) of \( g_{x} \) and \( g_{y} \) are a manifestation of the anisotropic exchange coupling (see Box 7) in the three-spin system and their values can be estimated from the spectrum.

5.1.2 Structural analysis of unusual Fe–S clusters (ZFS parameters, \( D \) & \( E \)).

Hydrogenases are enzymes that catalyse the interconversion of protons and hydrogen and are a benchmark for efficient \( H_{2} \) production with earth-abundant metals. HydG, an enzyme required for the assembly of [FeFe]-hydrogenases, harbours two [4Fe–4S] clusters. One of these is instrumental for the synthesis of the [FeFe] active site and can reversibly coordinate a fifth Fe atom yielding an unprecedented [5Fe–5S] cluster. The addition of a Fe\textsuperscript{2+} \( (S = 2) \) centre to a [4Fe–4S] cluster (with \( S_{\text{total}} = 1/2 \) in this case) generates a new spin system with total spin either \( S = 5/2 \) (ferromagnetic coupling) or \( S = 3/2 \) (antiferromagnetic coupling). The [5Fe–5S] and [4Fe–4S] clusters are readily distinguishable in the CW EPR spectrum: The high-spin [5Fe–5S] cluster (a mixture of \( S = 3/2 \) and \( 5/2 \)) appears at low magnetic field (Fig. 12A) whereas the low-spin [4Fe–4S] cluster \( (S = 1/2) \) appears around \( g = 2 \) (Fig. 12B).\textsuperscript{44} With the aid of the corresponding rhombogram for a \( S = 5/2 \) spin system (Section 2.6), the four effective \( g \) values observed for...
the [5Fe–5S] cluster are readily assigned: \( g = 9.5 \) arises from the \( m_s = \pm 1/2 \) manifold (i.e. one of the \( m_s = -1/2 \rightarrow m_s = +1/2 \) transitions)§ and \( g = 4.7, 4.1, 3.8 \) arise from the transitions within the \( m_s = \pm 3/2 \) manifold (i.e. \( m_s = -3/2 \rightarrow m_s = +3/2 \), in different orientations), from which the rhombicity can be determined as \( E/D = 0.225 \) (Fig. 12D). EPR spectroscopy thus provided evidence for the usual [5Fe–4S] cluster whose high-spin nature enabled its characterisation without interference from the low-spin [4Fe–4S] cluster.

### 5.2 Light induced phenomena

Time-resolved EPR (TREPR) enables the investigation of light-induced events such as photo-redox reactions, formation of photoexcited triplet states and radical pairs,\textsuperscript{45} and homolytic dissociation of chemical bonds. A laser flash generates the paramagnetic species (e.g. triplet or radical) and pulsed EPR experiments (i.e. detecting the electron spin echo, see Box 10) in the excited state can be performed as well as CW EPR. In this section, we provide an introduction to triplet-state EPR spectra and discuss examples. For further literature in the field, the reader is referred to ref. 46.

#### 5.2.1 Introduction to triplet-state EPR spectra

Let us consider a chromophore in its ground singlet state with an allowed optical absorption. Upon absorption of a photon, the chromophore is excited to its first excited singlet state. This can either decay back to the ground state (fluorescence or non-radiative decay) or cross to a triplet state via the intersystem crossing (ISC) mechanism. Triplet states are characterised by two unpaired electrons with parallel spins (\( S = 1 \)) with three corresponding triplet sublevels \( X, Y, Z \). The triplet sublevels are labelled as \( X, Y, Z \) in zero field and as \( 0, \pm 1 \) in high field (Fig. 13A and C). Since ISC is an anisotropic process, the transitions from the singlet excited state to the three triplet sublevels (and the decay rates from the three triplet sublevels to the ground singlet state) generally have different probabilities as determined by the molecular symmetry. Consequently, the populations of the triplet sublevels do not follow the Boltzmann distribution and are said to be spin polarised. Moreover, even in the absence of an applied field the energies of the triplet sublevels are usually non-degenerate and the relative splittings depend on the ZFS parameters (Section 2.6), as sketched in Fig. 13B. The corresponding transitions can be probed directly in zero-field and the most common way for organic triplet states is optically detected magnetic resonance.\textsuperscript{47}

When an external field is applied as customary in EPR, the electron Zeeman interaction also needs to be considered. Fig. 13C shows the energy level diagram for the simple case of the applied magnetic field parallel to the \( Z \) sublevel, in the assumption that the electron Zeeman interaction is much larger than all other interactions. The energy of this sublevel does not depend on the strength of the applied field, whereas the energy of the other sublevels mix and split proportionally to the applied field strength. Similar considerations apply to the

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§ Note that the other two \( g \) values are not observed because these are \(< 1\).
spin populations ($P_x$): $P_x$ is unaffected whereas the populations of the other two sublevels in high-field are the average of the corresponding populations in zero field. Similar energy-level schemes can be drawn for the applied field parallel to the X and Y axes of the ZFS tensor.

The TREPR spectrum of a photoexcited triplet presents some distinctive characteristics. First, the EPR spectrum features two allowed ($\Delta m_s = \pm 1$) transitions for each molecular orientation (Fig. 13C). Second, since the sublevels are spin polarised, both enhanced absorption and emission peaks are observed (Fig. 13D). When the sample is isotropic and all possible orientations are present (i.e. in a powder sample or frozen solution), the resulting 'powder average' spectrum (Fig. 13E) has six distinguishable turning points. From their positions, the magnitude (but not the sign) of the ZFS parameters can be derived. If $E = 0$ (i.e. $X = Y$) only four turning points are present.

5.2.2 Identification of energy transfer partners (electron spin polarization). Triplet excitation can be transferred from one site to another in a down-hill process. Photosynthetic light-harvesting complexes provide a prominent example when, under high light conditions, carotenoid triplet states are populated from chlorophyll triplet states in order to scavenge singlet oxygen. The electron spin polarization produced at the carotenoid acceptor site depends on the initial polarisation of the chlorophyll donor and on the relative geometrical arrangement of the donor–acceptor ZFS axes. This is because the triplet-triplet energy transfer mechanism occurs by an electron exchange mechanism with conservation of spin angular momentum. Therefore, the measured electron spin polarisation at the acceptor site (i.e. spectral shape) can be exploited to distinguish between competing donor–acceptor pairs, as it was shown for the peridinin–chlorophyll α–protein complex where a single chlorophyll is surrounded by 4 carotenoids.48a,b

Fig. 14 shows a comparison between the experimental TREPR spectra for the carotenoid and those calculated for each carotenoid–chlorophyll pair, taking into account the relative orientation of the two molecules. Clearly only the carotenoid labelled 614 gives a positive match and hence is responsible for quenching the chlorophyll triplet state.

5.2.3 Molecular wires (triplet exciton delocalization). Molecular wires, built on repeated units of π-conjugated monomers (such as porphyrins) are of interest for photonics, spintronics and molecular electronics applications. Tait et al.49 combined TREPR (to determine zero-field splitting parameters) and ENDOR (to measure proton hyperfine couplings) spectroscopies on photoexcited porphyrin linear oligomers (up to 6 units, Fig. 15A) to measure the extent of spatial delocalization of the triplet exciton.

For an evenly delocalized triplet, the ZFS parameter $D$ resulting from the spin–spin coupling of the unpaired electrons (see Section 2.7, Box 7) was expected to decrease proportionally to the number of units (i.e. the average distance). Unexpectedly, no significant change in the zero-field splitting parameters ($D$ and $E$) could be observed for linear oligomers with two to six porphyrin units (see Fig. 15B for a comparison of the monomer and dimer). In contrast, the spin polarization of the triplet state EPR spectra proved to be sensitive to the number of porphyrin units, demonstrating a different probability of populating the triplet sublevels with the number of units (Fig. 15B). In addition, the proton hyperfine couplings provided a highly reliable method to quantify the extent of the triplet delocalization: whereas delocalisation is complete in the dimer ($A_{\text{monomer}} = 2A_{\text{dimer}}$, Fig. 15C), the spin density is not distributed evenly over the whole π-system beyond the dimer (Fig. 15D). Hyperfine coupling constants can therefore reliably assess the extent of spin delocalisation. EPR spectroscopy proves a fundamental difference between excited singlet and triplets in linear porphyrin nanowires: while in the former the spin is evenly delocalised over the whole structure, in the latter it is localised over just the central porphyrin units.

5.3 Distance measurements

Pulsed dipolar spectroscopy constitutes a set of EPR experiments that enable the measurement of dipolar couplings between electron spins – naturally occurring or engineered as spin-labels – directly.

Fig. 14 Electron spin polarization as a source of structural information. (A) Pigment arrangement in the peridinin–chlorophyll α–protein. Green = chlorophyll, orange = carotenoids. (B) Experimental TREPR spectrum of the peridinin–chlorophyll α–protein at 150 K (black) with the corresponding calculated EPR spectra for each carotenoid surrounding the chlorophyll donor (in colour). Only two axes for the zero-field splitting tensors (black vectors) are shown for clarity (the third is orthogonal to both). $A = $ enhanced absorption; $E =$ emission. Adapted from ref. 48.
These experiments can involve a single microwave frequency, e.g. DQC (Double Quantum Coherence) and RIDME (Relaxation-Induced Dipolar Modulation Enhancement) or, in the vast majority of cases, two microwave frequencies. The latter two-microwave frequency experiment is known as DEER (Section 2.8.3), also known as PELDOR (Pulsed EElectron DOuble Resonance). Because the dipolar coupling is inversely proportional to the interspin distance cubed (Section 2.7, eqn (10), Box 7), pulsed dipolar spectroscopy provides information on the distance between electron spins. The technique has been applied to synthetic and biological systems alike, but is particularly suitable for dynamic systems too flexible to be crystallised or too large to be studied by NMR, and often complements other techniques, such as small-angle X-ray scattering or cryo-electron microscopy. Pulsed dipolar spectroscopy can assess distances between 1.8 and 8 nm (in fully deuterated media up to 13 nm) and not only provides an average interspin distance but also the distance distribution. Thus, it enables the characterisation of conformational distributions on a nanometer scale.

![Fig. 15](image1.png)

**Fig. 15** Triplet delocalisation in molecular wires of different lengths. (A) Molecular structure of the porphyrin moiety P where R = n-hexyl. (B) TREPR spectra of P1 (n = 1) and P2 (n = 2) at 20 K. (C) ENDOR spectra showing the hyperfine coupling A of the H2 protons (red circle in A) in excited P1 and P2. (D) Hyperfine couplings as a function of oligomer size (P1 to P6). The fitted line corresponds to the theoretical hyperfine couplings predicted for complete delocalization. Adapted with permission from ref. 49. A = enhanced absorption; E = emission. Copyright 2015 American Chemical Society.

![Fig. 16](image2.png)

**Fig. 16** Determining molecular wire lengths (distances) using DEER spectroscopy. (A) Molecular structure of the porphyrin wires (Pn), with n = 1 to 4; the nitroxide moieties are highlighted in blue. (B) Experimental time traces with fits (the periods for n = 1 and n = 4 are indicated by blue horizontal bars). The modulation periods for P1 and P4 are indicated by blue bars. (C) Distance distributions with equation relating inter-spin distance (r) and measured dipolar frequency (νdip). For a pair of nitroxide radicals, with g1 = g2 ≈ 2.0069, the equation can take the form 

\[ r = \frac{3}{4\pi} \frac{g1g2H_0}{4\pi\nu_{dip}} \]

(1) (where r is in nm) and it follows that at a dipolar frequency of ~52 MHz corresponds a distance of ~1 nm. (D) Comparison between DEER distances (data points) and crystallographic data (solid line). Adapted with permission from ref. 50. Copyright 2009 American Chemical Society.
Porphyrrin wires similar to those discussed above but labelled at both ends with stable nitroxide radicals (Fig. 16A) illustrate the inverse dependence of inter-spin distance and dipolar frequency. As shown in Fig. 16B, as the series progresses from one to four units (inter-spin distances 3.4 and 7.5 nm, respectively), the dipolar frequency measured through the DEER experiment decreases from ca. 1.3 MHz to 0.1 MHz (corresponding to modulation periods of ca. 0.8 and 7 μs, respectively). The resulting distance distributions are a manifestation of the rigidity and shape-persistence of such wires in solution (Fig. 16C) and indeed Fig. 16D shows that the inter-spin distances derived from EPR experiments are in excellent agreement with those estimated from crystallographic data. DEER can thus be used to measure nanometer distances reliably in disordered systems such as frozen solutions.

A full description of the theory behind pulsed dipolar spectroscopy and its applications is outside the scope of this tutorial review but can be found in ref. 51 and in the recently published chapters of eMagRes.14 For a review showcasing the latest developments in spin-labelling techniques for EPR distance measurements, with emphasis on the contribution of chemistry to the field, see ref. 52.

6 Concluding remarks

This tutorial review has highlighted some of the diverse problems that can be solved using various EPR spectroscopic techniques. We hope to have provided the reader with a basic set of tools and a foundation of the physical principles to tackle the interpretation of EPR data. We have seen that CW EPR involves observing transitions between electron spin states. On the other hand, pulse EPR enables access to transitions within electron-spin states and although the entire spin system may be complicated, different experiments can conveniently single out different interactions. A key point is that simulations are often essential in order to interpret EPR spectra and obtain accurate coupling parameters. Freely available simulation programs are becoming increasingly user friendly and satisfy the demands of the beginner as well as the expert user. It is important to emphasise that EPR spectroscopy often complements other methods, such as theoretical calculations. Technological developments in EPR spectroscopy are advancing quickly. Increasingly high-frequency/high-field spectrometers are becoming commercially available, and user-friendly bench top X-band instruments are able to satisfy the needs of many users. As the field and users of EPR spectroscopy expand, many new problems in the chemical sciences will be answered and we hope that this tutorial review has sparked the curiosity of the reader to explore the fascinating world of unpaired electrons.

Abbreviations

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<tr>
<th>Abbreviation</th>
<th>Description</th>
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<tr>
<td>CW</td>
<td>Continuous wave</td>
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<tr>
<td>$\nu_1$</td>
<td>Larmor frequency of a nucleus</td>
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<tr>
<td>$\nu_{mw}$</td>
<td>Applied microwave frequency</td>
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<tr>
<td>ENDOR</td>
<td>Electron nuclear double resonance</td>
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<tr>
<td>ESEEM</td>
<td>Electron spin echo envelope modulation</td>
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<tr>
<td>HYSCORE</td>
<td>Hyperfine sublevel correlation</td>
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<td>ZFS</td>
<td>Zero field splitting</td>
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<td>TREPR</td>
<td>Time-resolved EPR</td>
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<td>DEER</td>
<td>Double electron–electron resonance</td>
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<td>ISC</td>
<td>Intersystem crossing</td>
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Conflicts of interest

There are no conflicts to declare.

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