## Tutorial-5, Statistical Mechanics & Others (Paper-203), January 20,2016 Dr. R K Hazra Maximum Marks: 50

Q-1. Obtain  $E_{elec}$ ,  $A_{elec}$  and  $S_{elec}$  of a monoatomic gas. Discuss nuclear partition function of monoatomic gas. Calculate the fraction of He atoms in the lowest  ${}^{1}S_{0}$  state at  $300^{0}K$ and  $3000^{0}K$ .

Q-2. Find  $E_{tot}$  and  $A_{tot}$ . Obtain Sackur-Tetrode equation of  $S_{tot}$  of monoatomic gas.

Q-3. Find equation of ideal monoatomic, diatomic and polyatomic gases ( $\overline{p}V = Nk_BT$ ). Why  $'\overline{p}V = Nk_BT'$  does not differ for monoatomic and diatomic gases?

Q-4. Discuss briefly how nuclear spin (I) of a homonulcear diatomic molecule modulates rotational partition function?

Q-5. How many spin microstates  $H_2$  has? Write a short note on  $C_v$  of  $H_2$  gas at  $\sim 0^0 K$  and  $300^0 K$ ? Why cannot nuclear spin of  $H_2$  be inclusive as reciprocal of rotational symmetry factor  $\sigma$  at moderate temperature?

Q-6. Show that  $\hat{S}^2$  is an eigen-operator of  $o-H_2$  and  $(p-H_2)$ . Obtain their eigen-values.

Q-7. Find ' $\sigma$ ' of NO<sub>2</sub>, H<sub>2</sub>O, SO<sub>2</sub>, N<sub>2</sub>O, CO<sub>2</sub>, COS (diagrams).

Q-8. Find  $E_{rot}$  and  $C_v$  of polyatomic gas at moderately high temparatue.

Q-9. Find  $S_{rot}$  of polyatomic gas at moderately high temparatue.

Q-10. Find  $E_{tot}$ ,  $C_v$  and  $S_{tot}$  of a polyatomic gas at moderately high temparatue.

Q-11. Prove that  $\overline{p}V = k_B T \ln(Z(v, T, \mu))$  of a grand-canonical ensemble. What are thermodynamic characteristic functions of different ensembles?

Books: McQuarrie (Statistical Mechanics), Callen (Thermodynamics and Thermostatistics),

Nash (Elements of Statistical Thermodynamics), Atkins (Physical Chemistry), Landau & Lifshitz (Statistical Physics), MC Gupta (Statistical Mechanics).